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1 **VISUALISATION AND LES SIMULATION OF CAVITATION CLOUD FORMATION AND**
2 **COLLAPSE IN AN AXISYMMETRIC GEOMETRY**

3
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15 **ABSTRACT**

16 Visualization and Large Eddy Simulations (LES) of cavitation inside the apparatus previously
17 developed by [1] for surface erosion acceleration tests and material response monitoring are
18 presented. The experimental flow configuration is a steady-state closed loop flow circuit where
19 pressurised water, flowing through a cylindrical feed nozzle, is forced to turn 90 degrees and then,
20 move radially between two flat plates towards the exit of the device. High speed images show that
21 cavitation is forming at the round exit of the feed nozzle. The cavitation cloud then grows in the radial
22 direction until it reaches a maximum distance where it collapses. Due to the complexity of the flow
23 field, direct observation of the flow structures was not possible, however vortex shedding is inferred
24 from relevant simulations performed for the same conditions. Despite the axisymmetric geometry
25 utilized, instantaneous pictures of cavitation indicate variations in the circumferential direction. Image
26 post-processing has been used to characterize in more detail the phenomenon. In particular, the mean
27 cavitation appearance and the cavity length have been estimated, showing good correlation with the
28 erosion zone. This also coincides with the locations of the maximum values of the standard deviation
29 of cavitation presence. The dominant frequency of the 'large-scale' cavitation clouds has been
30 estimated through FFT. Cloud collapse frequencies vary almost linearly between 200 to 2000Hz as
31 function of the cavitation number and the downstream pressure. It seems that the increase of the
32 Reynolds number leads to a reduction of the collapse frequency; it is believed that this effect is due to
33 the agglomeration of vortex cavities, which causes a decrease of the apparent frequency. The results
34 presented here can be utilized for validation of relevant cavitation erosion models which are currently
35 under development.
36

37 **Keywords:** cavitation, erosion, collapse, LES
38

39 **1. INTRODUCTION**
40

41 Understanding and controlling cavitation has been a major challenge in engineering for many years.
42 Cavitation erosion is generally believed to be the result of violent collapses of the flowing cavitation
43 micro-bubbles within very short time scales [2]; it often leads to vibration and damage of mechanical
44 components, for example, marine propellers and rudders, bearings, fuel injectors, pumps and turbines.
45 Studying the sheet/cloud cavitation is important to understand the causes of cavitation erosion, and to
46 predict accurately its aggressiveness in terms of erosion risks, or even more, damage rate. In [3] a
47 review of the physical mechanisms for cavitation erosion loads is given. These mechanisms are
48 evaluated with observations on the detailed dynamics of the flow over a cavitating hydrofoil and with
49 observations that are available from ships where cavitation has led to erosion damage on the rudder or
50 the propeller. Many recent studies (selectively [1, 4-14]) have examined the time dependent
51 progression of cavitation erosion for different materials. Due to the aforementioned detrimental
52 effects of cavitation on hydraulic equipment, most of experimental research has focused over the
53 years on methods with which cavitation damage could be quantified and linked to measurable

54 material properties. In [15], systematic cavitation erosion tests have been performed on a water
55 hydraulic system; results from this study have been reported in the past and have been widely used for
56 benchmarking relevant computational fluid dynamics and cavitation erosion models. Briefly, it was
57 shown that cavitation erosion during the incubation period was occurring via pitting. Cavitation
58 damage was not correlated with the elastic limit determined from conventional tensile tests and it is
59 conjectured that other parameters such as the strain rate might play a significant role. However, the
60 flow details associated with the erosion tests have not been recorded.

61
62 At the same time, many studies have been reported on flow visualisation in cavitating flows in a
63 number of devices. A review on numerical and experimental investigation of sheet/cloud cavitation
64 was carried out by [16]. Sheet/cloud cavitation could influence the dynamic flow pattern. In [17] a
65 numerical and experimental investigation of sheet/cloud cavitation on a hydrofoil at a fixed angle of
66 attack is reported. The results show that, for the unsteady sheet/cloud cavitating case, the formation,
67 breakup, shedding, and collapse of the sheet/cloud cavities increase the turbulent intensity, and are
68 important mechanisms for vorticity production and modification. Another important feature of the
69 problem is the lift oscillations due to the highly periodic nature of the sheet/cloud cavitation. In [18] it
70 was found that the dynamic characteristics of the cavitation vary considerably with various
71 combinations of angle of attack and cavitation number, σ . At higher angles of attack, two types of
72 flow unsteadiness are observed. At low σ , there is a low frequency shedding of cloud cavitation
73 observed at a Strouhal number of about 0.15. This non-dimensional number is relatively insensitive to
74 changes in σ . As σ is raised, the sheet frequency varies almost linearly with cavitation number.

75
76 A recent study by [19] was focused on the simultaneous observation of cavitation structures and
77 erosion, in order to find a pattern linking the evolution of cavities with the erosion development. The
78 studies were conducted in a cavitating Venturi nozzle section, where part of the nozzle was covered
79 by a thin aluminium foil; this enabled the rapid accumulation of erosion pits and allowed the
80 observation of the erosion development, since the rest nozzle walls were transparent. From the
81 observations, it was concluded that, while the exact volume and distance of the vapour cavity does not
82 play a significant role to erosion damage, extensive erosion was caused by the collapse of uneven and
83 asymmetrical vapour cavities. The authors hypothesize that erosion might be caused by two
84 mechanisms (or a combination of both): a) the shock wave generated by the cloud collapse is
85 triggering the collapse of microbubbles in the vicinity of the wall area b) the irregular shape of the
86 cavitation cloud causes asymmetrical, non-spherical shock waves that have a distinct orientation.

87
88 Along these directions, a number of computational studies on cavitation have been reported over the
89 years. Direct numerical simulation of the whole process is computationally very demanding but
90 provides a good insight into the relevant mechanisms and physics. One notable example of a DNS
91 study of the collective bubble collapse is the recent work of [20], where the authors employed massive
92 parallelism to simulate a cluster of 15,000 bubbles collapsing near a wall, utilizing a grid with size of
93 13 trillion cells. Of course the resources required to run such a simulation are prohibitive for industrial
94 application; for the specific application the authors utilized a supercomputer consisting of 1.6 million
95 cores, which obviously is impractical to use in everyday engineering computations.

96
97 Another approach to simulate the effects of erosion is by including the exact behaviour of the fluid,
98 using a complicated equation of state that reproduces the phase diagram of the liquid/vapour phases.
99 This approach has been followed in [21], who employed a density based solver with shock capturing
100 schemes to simulate the cavitation in the same geometry described in the current paper. Erosion is
101 predicted in the form of shock waves, which originate from the collapse of vapour structures. The
102 simulation methodology, though, had the limitation of small time steps, due to the inclusion of
103 compressibility effects for both liquid and vapour phases.

104
105 Considering the above, it becomes obvious that, even if there are state of the art methodologies
106 capable of potentially accurate representation of the behaviour of cavitation structures, their

107 application in everyday problems is limited, due to vast amount of computational resources they
 108 require. Thus, in practice, a significant effort is put to derive semi-empirical models to describe the
 109 cavitation erosion, which is inherently related to the micro scale effects. Typically, the large-scale
 110 problem can be addressed by e.g. multi-phase RANS/LES solvers while the micro-scale problem can
 111 be addressed by either a numerical model [22, 23], or by a semi-empirical erosion model or damage
 112 functions [24-26]; along these lines, validation against experimental erosion data is of significant
 113 importance. Here it should be highlighted that various researchers [24, 27, 28] have found that
 114 traditional URANS models suffer from a deficiency in predicting the shedding frequency of cavitating
 115 flows; the proposed methodologies to treat this deficiency is either to modify the turbulent viscosity
 116 formulation of the traditional URANS models, or employ hybrid RANS/LES or pure LES
 117 methodologies.

118
 119 The present contribution aims to provide more insight to the details of the cavitation sheet/cloud
 120 developing in a purpose build device that has been previously used for extensive cavitation erosion
 121 measurements[15]. In this paper the same apparatus is used to visualise the cavitating flow in an effort
 122 to correlate the observed cavitation erosion locations with the location of cavitation development. The
 123 next section of the paper gives a short description of the experimental apparatus used, followed by a
 124 brief description of the computational model; then the presentation of the obtained results follows
 125 while the most important conclusions are summarised at the end.

126 127 **2. EXPERIMENTAL SETUP**

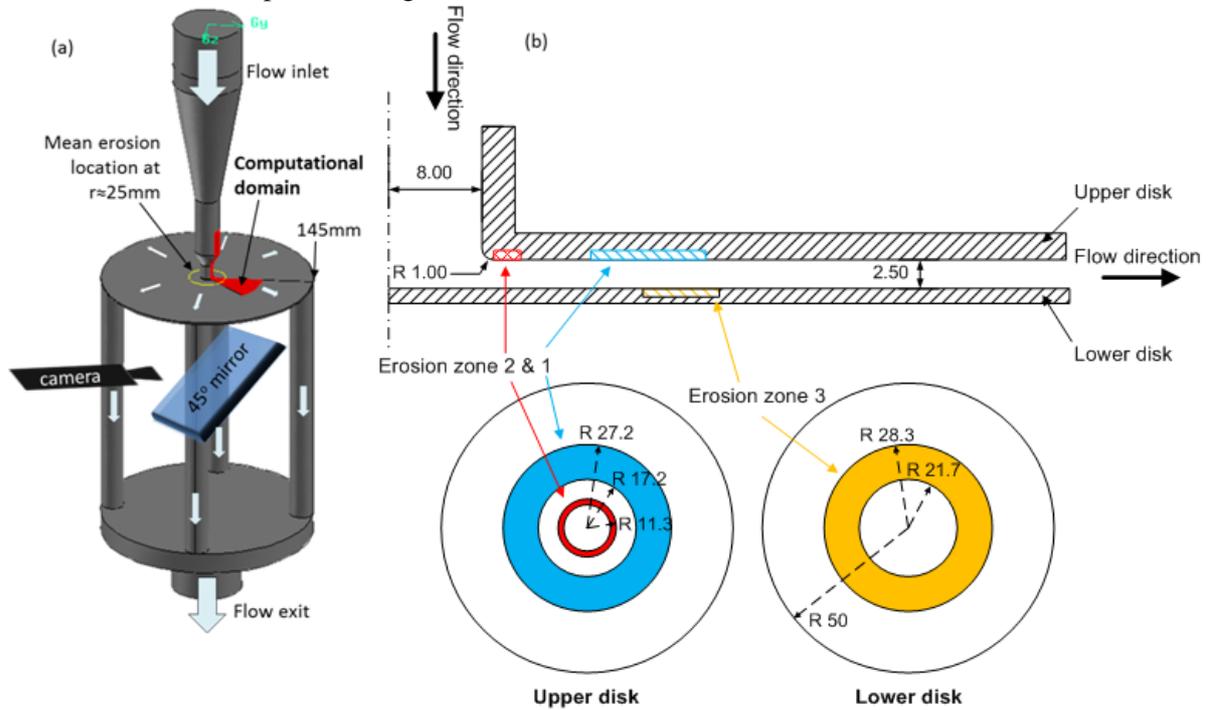
128
 129 As already mentioned, the experiments were conducted in a cavitation flow loop described in detail
 130 in[15]. The test section is axisymmetric and made of a straight feed nozzle with 16mm diameter. The
 131 flow is accelerated by two converging nozzles with cross-section ratios of 2.86:1 and 2.12:1 and
 132 lengths 178 and 80mm respectively. As illustrated in Fig. 1, the flow is deflected by the sample to be
 133 eroded which is set at a distance of 2.5mm from the nozzle exit. It then moves radially within the
 134 2.5mm gap formed between the sample and the nozzle exit orifice. The radius of curvature of the feed
 135 nozzle exit was 1mm. The working fluid was tap water kept at fixed temperature of 25°C. Cavitation
 136 erosion data are only available for a cavitation number of 0.9, showing three distinct and clearly
 137 separated cavitation erosion sites: two at the upper surface and one of the lower surface. On the upper
 138 surface, cavitation erosion is observed just at the turning location of the flow where cavitation is
 139 generated and then a few mm further downstream. A cavitation erosion free zone between them
 140 exists. On the lower surface, erosion has been observed only at the closure region of the cavity in the
 141 form of a circular ring whose mean radius is around 25mm[15].

142
 143 The test section is placed in a closed circuit comprised by different equipment: centrifugal pump, heat
 144 exchanger, test section, electromagnetic flowmeter. The centrifugal pump of 80kW is driven by a
 145 variable speed motor. It can provide a pressure of 40bars and a maximum flow of 11l/s. The flow
 146 through the system is measured using an electromagnetic flow meter. A heat exchanger allows
 147 maintaining the water temperature constant. The maximum operating pressure of the circuit is 40bars,
 148 which corresponds to a mean velocity of 65m/s at the turn located at the nozzle exit, calculated at the
 149 peripheral surface of the cylinder with height 2.5mm and radius 8mm. The pressurization of the
 150 system is supported by means of a balloon located downstream the test section. A pressure control
 151 device is used to finely control this downstream pressure (P_{down}) in the installation. Various pressure
 152 and temperature sensors are used to determine precisely the test conditions. Here it is important to
 153 mention the definition of the cavitation number σ , used in the present paper:

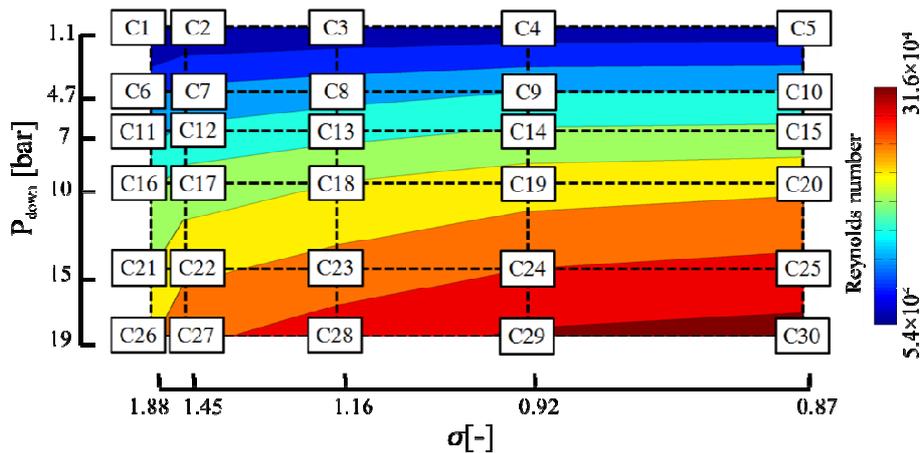
$$154 \quad \sigma = \frac{P_{down} - P_v}{P_{up} - P_{down}} \approx \frac{P_{down}}{P_{up} - P_{down}}$$

155 where P_{down} and P_{up} are the static pressures upstream and downstream the test section and P_v is the
 156 vapour pressure of the liquid at the temperature of the experiment.

158 To visualize the cavitating flow the metal sample was replaced with a sample made of Perspex with
 159 suitable thickness to withstand the working pressure (see Fig. 1). A 45° mirror was fixed in front of the
 160 Perspex allowing for cavitation images to be collected by a high speed camera (Phantom®
 161 MiroM320S). The optic used was a Tamron® AF 90mm f/2.8 SP Di macro-lenses. As one camera
 162 was available and optical access was restricted by the design of the flow rig, only bottom view images
 163 could be collected. Thus, any three dimensional effects developing within the 2.5mm gap could not be
 164 identified; the images and their post-processing can only reveal the projected view of the cavitation
 165 cloud on the imaging plane. Two lights (Lupo® Spot Daylight 1200) were placed behind the mirror
 166 and in front of the Perspex allowing for sufficient illumination.



167
 168 **Fig. 1:**(a) Sketch of the visualization apparatus from [15]. (b) Zoom-in to the area of interest; the
 169 dimensions of the three distinct erosion zones observed are indicated in mm, for $\sigma=0.9$.
 170



171
 172 **Table 1:**The 30 test cases investigated. For each case, the experiment was conducted at fixed P_{down}
 173 and σ values. Note that both the p-axis and σ -axis are inverted. The Reynolds number is calculated
 174 between the two disks at $r=25$ mm - see Fig. 1, based on the hydraulic diameter ($D_h=5$ mm). The six
 175 cases at $\sigma = 1.88$ are not included in the experimental results, because a coherent cavitation cloud was
 176 not formed.
 177

178 The area visualised was $34 \times 16 \text{ mm}^2$, so the pixel size was $132 \times 125 \mu\text{m}^2$. This pixel size introduces an
179 uncertainty of 0.4% ($0.132/34$) in the relative spatial resolution of the collected images. The videos
180 were recorded at 77kHz with a resolution of 258×128 pixels. In total, more than 2000 frames have
181 been collected for each operating condition. The exposure time was set to $12 \mu\text{s}$; during that time the
182 cavitation could move by less than 0.012mm, which is much smaller than the pixel resolution;
183 practically this shutter time freezes the motion of the cloud. Visualisation tests were conducted at
184 different cavitation numbers, σ from 0.8 to 1.90 and back pressures, P_{down} from 1.1bar to 19.1bar. The
185 matrix of the test cases recorded is shown in Table 1. Flow conditions at the highest cavitation
186 number ($\sigma \sim 1.9$) correspond to cavitation inception at the given upstream and downstream pressure
187 difference. Those cases are listed here for completeness although they have been excluded from the
188 analysis to follow, as the cavitation cloud formed was very irregular and restricted to small cavitation
189 pockets without any erosion data being reported. The Reynolds number indicated with the contour
190 plot has been calculated on the basis of the hydraulic diameter of the 2.5mm passage and the mean
191 flow velocity estimated at a radial distance of 25mm. From those conditions, the effect of σ and P_{down}
192 can be evaluated separately. In this Table the numbering of the cases tested, from C1 to C30 is also
193 indicated and this notation is used throughout the paper.

194 195 **3. Flow structure and post processing methods**

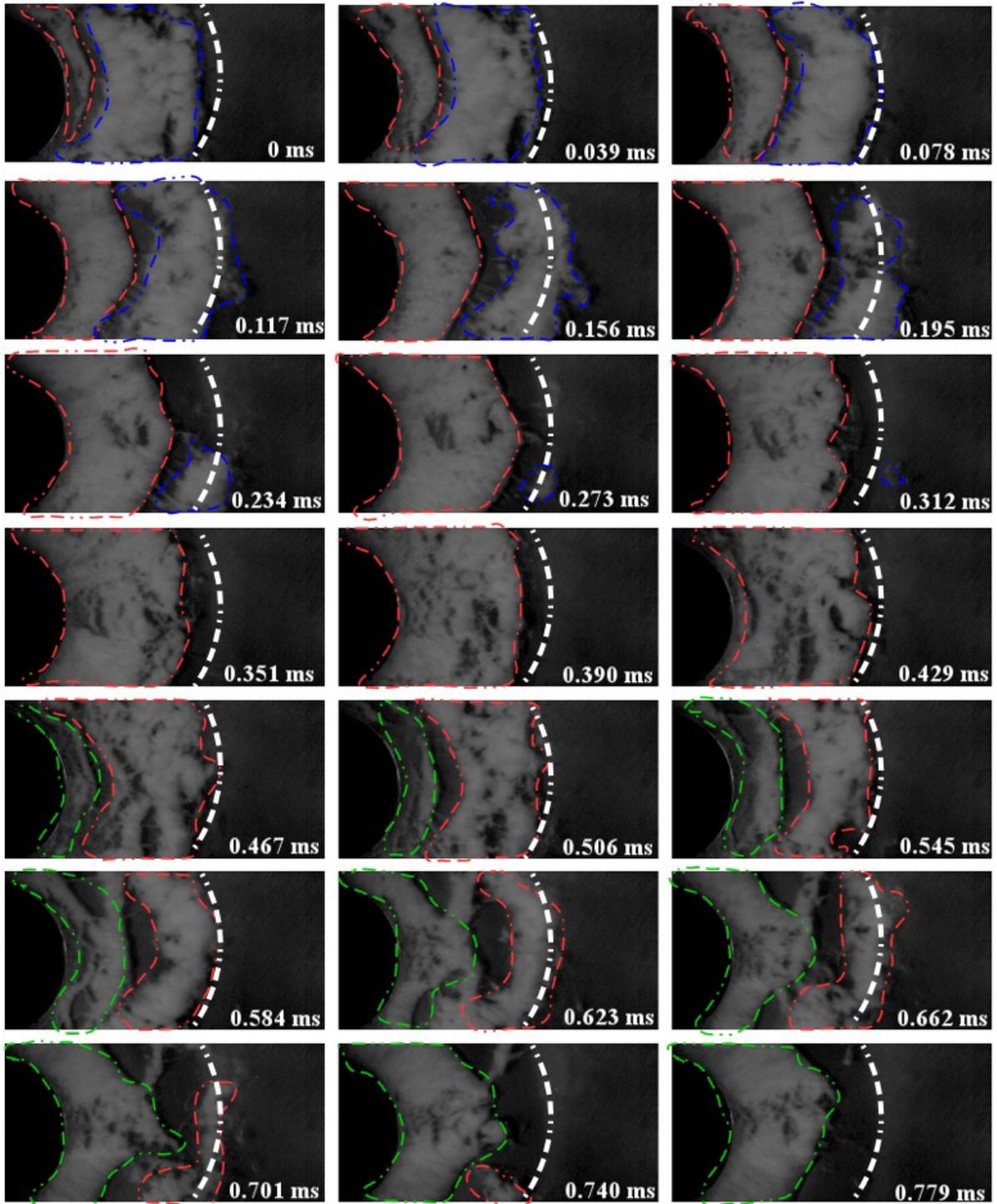
196 The cavitation cloud was found to change location rather transiently and non-axisymmetrically
197 despite the steady-state operation and the axisymmetric geometry utilized; a typical sequence of the
198 cloud formation and development is shown in Fig. 2. This figure shows representative images selected
199 from case C29 of Table 1; this case corresponds to the erosion tests and sites described previously.
200 The cloud is generated at the outlet of the feed nozzle; this has been a consistent observation for all
201 cases recorded. Then the cavitation cloud grows as it is convected by the flow, until it reaches a
202 maximum distance; this corresponds to the time frame of 0.117ms in Fig. 2. Upstream of this ‘large-
203 scale’ cloud structure, which is indicated by the blue dotted line, a second ‘large-scale’ cloud,
204 segmented by the red line is developing, flowing downstream in a similar manner. A cavitation-free
205 zone is visible between them. The follow-up cloud is indicated by the green line and the process
206 repeats itself in a clear vortex shedding mechanism. The estimated shedding frequency is of the order
207 of 1 to 2 kHz for this particular test case; more details about the cloud collapse frequencies are
208 assessed later on.

209
210 Having described the dominant flow structures, image post processing has been employed in an effort
211 to provide estimates of parameters relevant to the spatial and temporal development of the cavitation
212 clouds. To do that, the single-colour (grey-scale) images of cavitation recorded (a representative
213 image is shown in Fig. 3a) are turned to binary ones; an example is shown in Fig. 3b. This has been
214 achieved by utilizing the Otsu's method [29]; the threshold value chosen aims to minimize the
215 interclass variance of the black and white pixels. Two averaging procedures have been performed: (a)
216 per pixel and (b) along the circumferential direction, as indicated in Fig. 3b. The field of view
217 analysed is an annular sector with radii $8 \text{ mm} < r < 30 \text{ mm}$ and angle θ of 30 degrees. This zone has
218 been divided into 260 concentric arcs.

219
220 At the outlet of the feed nozzle, light reflection on the radius of curvature may not be distinguished
221 from the automatic process converting the raw images to binary ones. For this reason, this area has
222 been masked up to a radial distance of 9.5mm and the corresponding pixels found in this angular zone
223 have not been considered in the post-processing. For the point (pixel) averaging, the temporal mean
224 cavitation presence and its standard deviation have been estimated and contour plots similar to Fig. 3c
225 will be presented in the following section. The mean value can be interpreted as the % number of
226 frames when cavitation is present in a particular location while the corresponding values of standard
227 deviation indicate locations where unsteady cavitation develops.

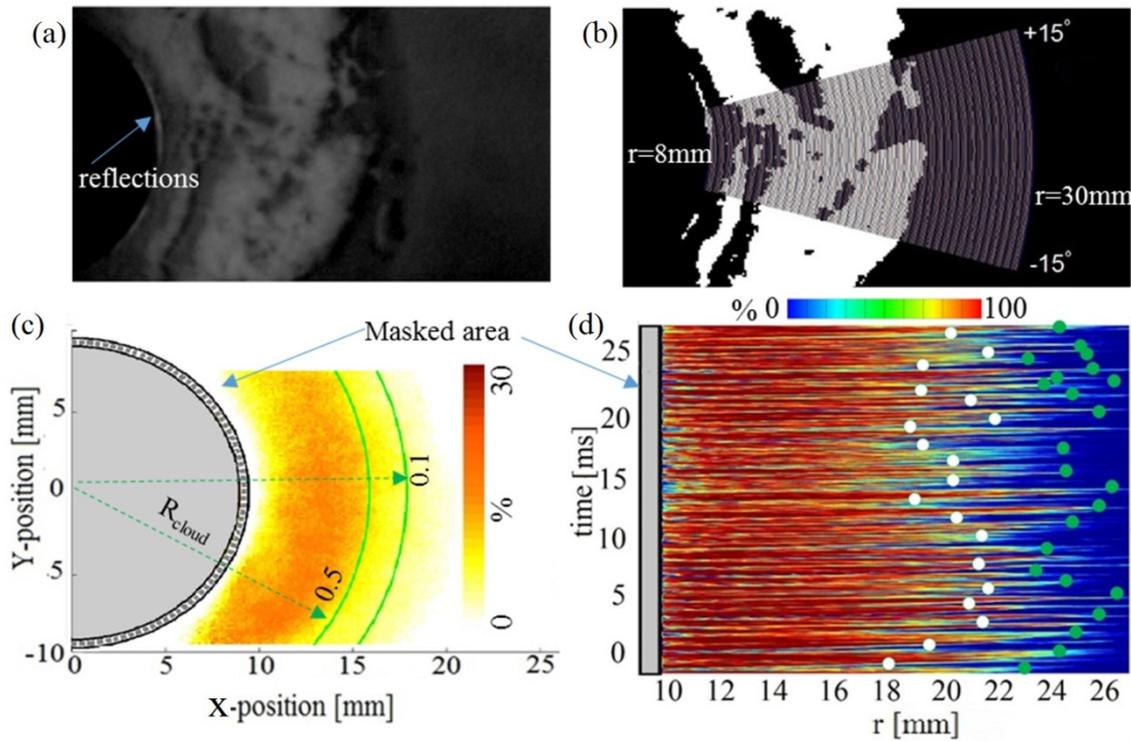
228
229 Obviously, an error is introduced by the threshold value when performing this process. As possible
230 acceptable threshold values can range between two extremes, the maximum relative error can be

231 estimated and its spatial distribution is shown by the contour plot of Fig. 3c for case C27; this case has
 232 been selected as it exhibits less cavitation, and it has been found to have the maximum error among all
 233 cases investigated. It can be seen that the error can take value of up to 20% relative to the mean value
 234 of this particular case. The peak values exist in the central part of the cloud development as in these
 235 areas it is less accurate to draw clear boundaries between the cavitating and the non-cavitating areas.
 236 This error decreases with increasing radial distance and becomes smaller than 5% in the area of cloud
 237 collapse.



238
 239
 240 **Fig. 2:** Sequence of representative images captured using a frame rate of 77k frames per second
 241 (termed as fps from now on), C29 ($P_{down} = 19$ bar, $\sigma = 0.92$). The white dashed line indicates the

242 distance of 25mm from the axis of symmetry, which corresponds to the mean distance where erosion
 243 sites 2 and 3 have been observed. The coloured dashed lines follow the edge of successive cavitation
 244 clouds.
 245



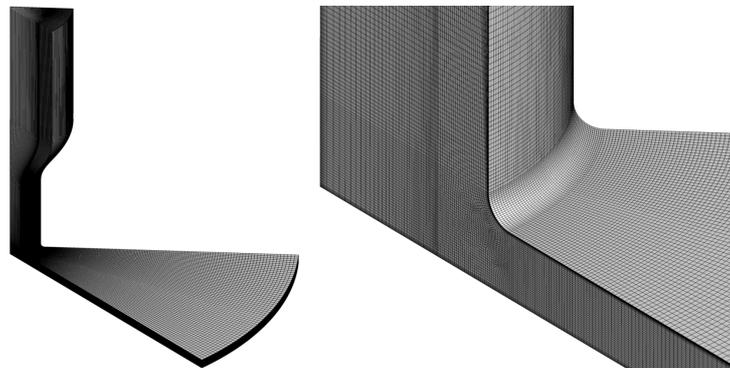
246 **Fig. 3:** (a) Representative raw image, (b) binary image after applying a threshold method; the
 247 circumferential sectors utilised for post-processing are superimposed. (c) Representative spatial
 248 distribution of relative error of the mean cavitation presence in every pixel visualised for case C29;
 249 the green lines indicate the cloud length by utilising two different threshold values of 0.5 and 0.1 for
 250 its estimation. (d) Representative plot of temporal evolution of the % circumferential area occupied by
 251 cavitation as function of distance from the axis of symmetry; the superimposed green circles indicate
 252 the locations of maximum cloud extend at the start of collapse and the white circles indicate the cloud
 253 length at the end of collapse.
 254

255
 256 The second image post-processing method employed estimation of averages along the circumferential
 257 direction. This time, the mean of the binary values along each arc has been obtained for every time
 258 instant recorded; this can be simply expressed as $N_1 / (N_0 + N_1)$, where N_0 is the number of pixels
 259 exhibiting zero value (no cavitation presence) and N_1 is the number of pixels with value equal to one
 260 along the selected areas. This ratio represents the percentage area of this circumferential sector
 261 occupied by cavitation at a given time step. A representative result from this process is shown in Fig.
 262 3d. A few sample points (for clarity of the plot), indicated by the white and green circles, have been
 263 superimposed. These circles correspond to radial distances where the mean of the binary values across
 264 a circumferential sector has a value of 0.5, indicating that half of this sector is occupied by cavitation
 265 at a given time step. This parameter can be utilised to estimate the cloud length at the beginning and
 266 ending of the collapse phase. The white circles correspond to time instances at the end of the collapse
 267 phase while the green circles at the start of the collapse when the cloud has its maximum extent. By
 268 averaging the radial locations corresponding to these two time events, one can obtain the mean of the
 269 maximum and minimum cloud extend over all collapse cycles recorded. This is defined here as 'cloud
 270 length', and represented with R_{cloud} , and its variation for all cases is presented later on. The maximum
 271 value of R_{cloud} is also indicated on Fig. 3c by the green lines superimposed on this plot for this
 272 particular case C27. The one to the left has been estimated by using a value of 0.5. Obviously, other
 273 values towards zero could have been selected. However, with smaller values one may capture only

274 small clouds isolated from the main cavitation area, and which may not be representative of the mean
275 value across the whole circumferential area. As it is impossible to have an ‘accurate’ estimate, a
276 relative error has been estimated by using a value of 0.1 (implying that only 10% of the
277 circumferential sector is occupied by cavitation at a given time). The value calculated from this
278 assumption is also indicated on Fig. 3c. It can be seen that the cloud length in this case is
279 approximately 2.5mm further downstream relative to the value estimated when 0.5 was used. This
280 gives a relative error of approximately 15% for this particular case. It decreases in cases with more
281 cavitation to levels of around 1-1.5mm which corresponds to about 7% of the cloud length. Finally,
282 fast Fourier transformation (FFT) applied to the temporal evolution of this cloud length can reveal the
283 ‘large-scale’ cloud collapse frequency.
284

285 4. CFD Simulations

286 In the absence of quantitative velocity measurements in this configuration, CFD simulations have
287 been performed to provide more insight to the flow structure. The described case was simulated using
288 the in-house CFD solver, GFS. The solver is based on the finite volume methodology. The liquid
289 phase is considered as an incompressible liquid and is resolved in an Eulerian reference frame,
290 whereas cavitation is treated as a discrete phase tracked in Lagrangian frame of reference [30]. The
291 bubble motion is governed by the forces due to bubble/liquid interaction, whereas appropriate source
292 terms are added in the continuous phase conservation equations to take into account the effect of the
293 bubble presence inside the liquid flow. The bubble size is governed by the Rayleigh-Plesset equation
294 [30]. The bubble number density for the cavitation inception was set to 10^{13} bubbles/m³, with a size
295 ranging from 0.5µm to 2µm, following a logarithmic distribution; the aforementioned values are
296 based on literature references [30, 31] and are considered representative of feed water. Since
297 simulating explicitly all bubbles inside the volume would require enormous computational resources,
298 parcels of bubbles are simulated; all bubbles within a parcel are assumed to behave in exactly the
299 same way, thus they have the same velocity field and bubble radius and parcels are introduced in
300 regions where the local pressure is below the saturation (the interested reader is addressed to [30]). In
301 the present simulations the maximum number of bubble parcels was ~45000. The solver is capable of
302 predicting the flow pattern of the fluid/vapour mixture, but, even if the bubbles may expand or
303 collapse, cannot handle compressibility effects and pressure wave propagation in the bubbly medium.
304



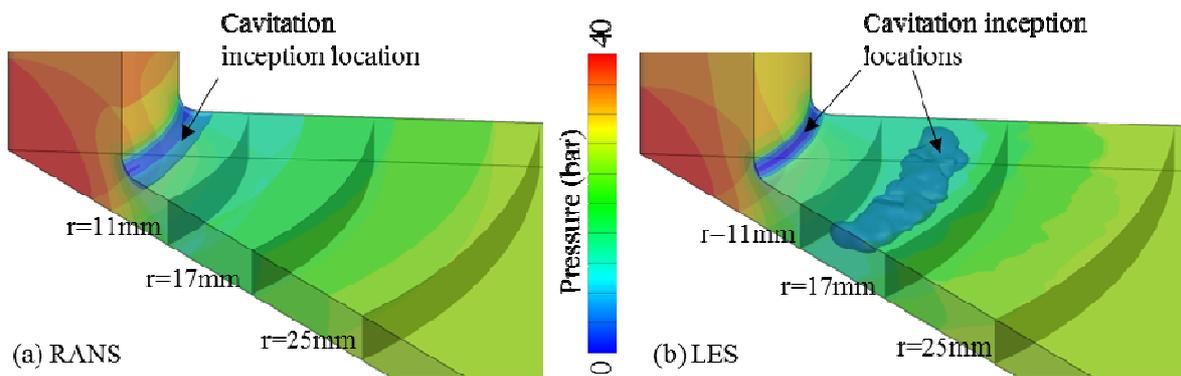
305 **Fig. 4:** Computational grid utilized for the CFD analysis; the grid consists of 1.4million cells and has
306 a higher density at the cavitating region
307
308

309 The simulation performed with GFS was done with a hybrid RANS/LES model [32-34], since it was
310 found that standard traditional URANS models fail to predict the vortex shedding mechanism, while
311 also underestimate the size and the extents of the cavity; this is supported also from other CFD studies
312 in the literature [27, 28]. Moreover, computational predictions with the RANS/LES model suggest the
313 existence of a secondary nucleation site downstream the turn; such fine features are not captured by
314 standard RANS models, as e.g. the k-epsilon model (see Fig. 5 -the comparison is made after
315 obtaining a steady state solution using the k-epsilon model, whereas an average solution has been
316 extracted from the transient hybrid RANS/LES approach, after sampling 550 time instances). While

317 the prediction of a secondary nucleation site cannot be verified by experimental observations, due to
 318 the complexity of the flow field, the prediction of this site may contribute to the understanding of the
 319 underlying mechanisms of cavitation development and suggests further examination in future
 320 experiments. The predicted location of the second inception site is within the erosion free zone, lying
 321 between 11.3 and 17.2mm (see also Fig. 1), could be considered as a rough indication of agreement
 322 between the CFD and the experimental results. It must be highlighted here that it is not implied that
 323 the secondary cavitation inception region, downstream the turn, is a stationary vortex core; it appears
 324 in such a way, due to the time averaging process for many time instances. In practice, the secondary
 325 inception site is a highly dynamic and transient feature, generated by the high vorticity downstream
 326 the turn, spanning from a radius of 9 to 20 mm, see also **Σφάλμα! Αγνώστη παράμετρος**
 327 **αλλαγής.** and Fig. 10. This area has the form of a Rankine vortex, with a characteristic size of
 328 ~1.5mm. In order to simplify the simulation and decrease the computational cost, due to spatial and
 329 temporal resolution requirements of the turbulence model used, only 1/8th of the complete geometry
 330 was simulated (see Fig. 1). The computational mesh used consists of approximately 1.4million purely
 331 hexahedral cells, refined near the walls and the inlet sharp turn at the feed nozzle exit as showed in
 332 Fig. 4. The minimum cell size in the near wall vicinity is 2μm and the maximum dimensionless wall
 333 distance (y^+) in the area of interest is ~10. From the results obtained, it was tested that the turbulent
 334 kinetic energy spectrum obeys the Kolmogorov -5/3 law [35] and the highest temporal frequency was
 335 at least 10 times less than the sampling frequency; thus both the temporal and spatial discretizations
 336 were considered adequate for the simulations. The simulated condition was for $P_{up}=40\text{bar}$ and
 337 $P_{down}=19\text{bar}$ (pressure difference 21bar), corresponding to a flowrate of 8.16 l/s and a cavitation
 338 number of 0.92 (case C29 of Table 1). The discharge coefficient C_d , defined as:

$$339 \quad C_d = \frac{Q_{CFD/Exp.}}{\sqrt{\frac{2(P_{in} - P_{out})}{\rho \left(\frac{1}{S_{out}^2} - \frac{1}{S_{in}^2} \right)}}}$$

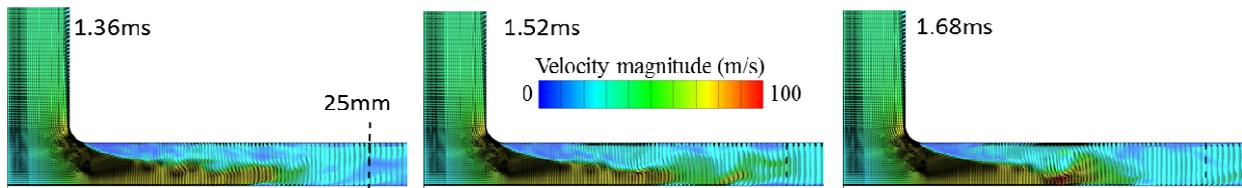
340 is ~0.13 for the cavitating case. Simulating the same case and ignoring cavitation effects results to a
 341 significantly lower pressure difference prediction of ~13bar ($C_d \sim 0.16$) instead of 21bar (reduction of
 342 38%).
 343



344 **Fig. 5:** Comparison of the pressure field from the RANS and the hybrid RANS/LES (averaged in
 345 time). The blue iso-surface denotes the region where pressure drops below saturation pressure. The
 346 simulation conditions correspond to C29, with $\sigma \sim 0.9$ and $P_{down}=19\text{bar}$.
 347
 348

349 In Fig. 6 the velocity field at a slice of the computational domain is shown. The velocity field is
 350 highly unsteady, with vortices formed downstream the sharp turn, in the shear layer that develops at
 351 the boundary of the separated region. Pressure at the vortex cores drops below the saturation pressure,
 352 leading to the formation of vapour cavities, which travel downstream forming the cavitation clouds, in
 353 a similar pattern as shown from experimental results.

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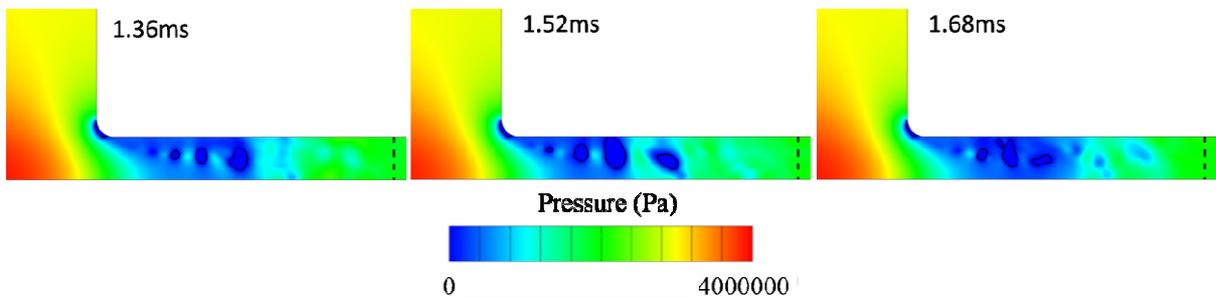


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Fig. 6: Velocity distribution at three instances with a time interval of $60\mu\text{s}$, taken at the middle slice of the simulated geometry. The simulation conditions correspond to C29, with $\sigma\sim 0.9$ and $P_{down}=19\text{bar}$.

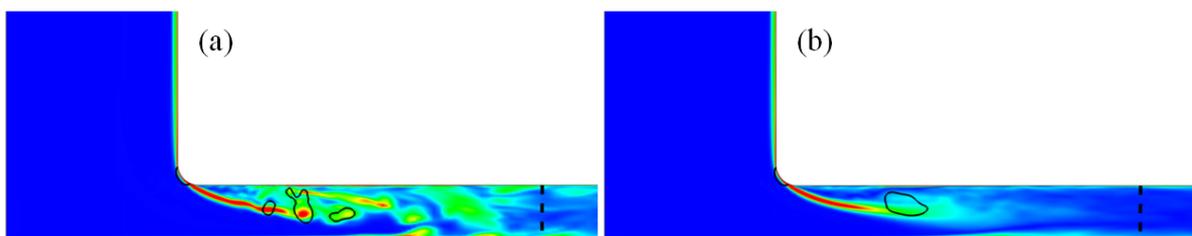
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In Fig. 7 the instantaneous pressure distribution in the gap between the two disks is shown. Evidence of travelling vortices can be found here; as shown, pressure drops below saturation at the vicinity of the turn (primary inception point) and at the vortices formed due to the shear layer instability, downstream the turn. Collectively, these vortices act as the secondary nucleation site mentioned above. In both nucleation sites, bubble parcels are introduced, in order to take into account vapour presence in the flow field.



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Fig. 7: Instantaneous pressure distribution at three instances with a time interval of $60\mu\text{s}$, at the middle slice of the simulated geometry. The continuous line denotes the region where local pressure is below the saturation pressure and the dashed line the radius of 25mm.

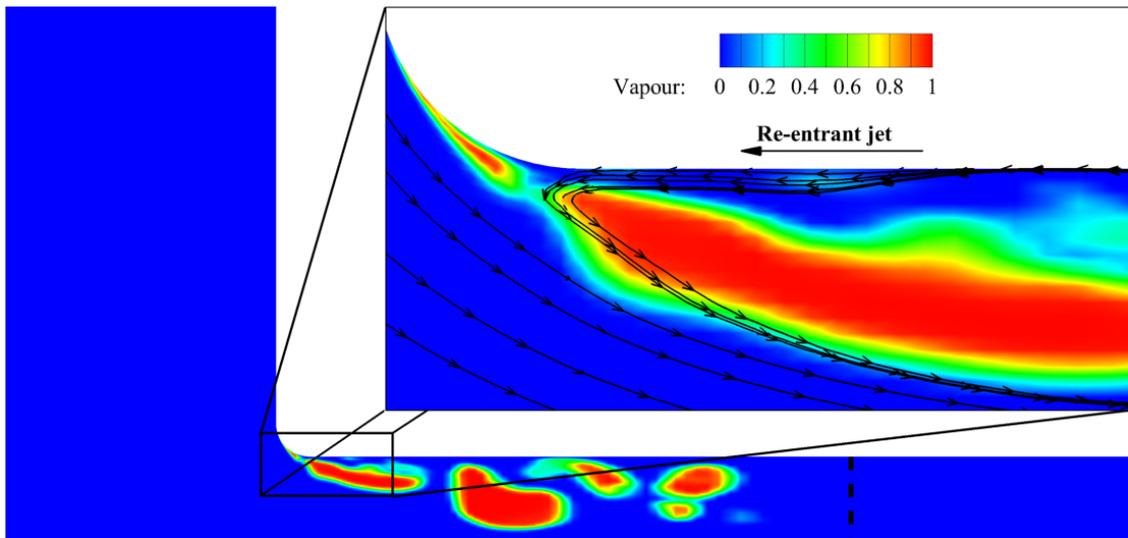


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Fig. 8: (a) Instantaneous and (b) time-averaged vorticity magnitude fields. The continuous line shows the inception sites, with local pressure lower than the saturation pressure, whereas the dashed line indicates the radius of 25mm. Note that, due to interpolation during the slice extraction, smoothing is inevitably introduced to the vorticity field.

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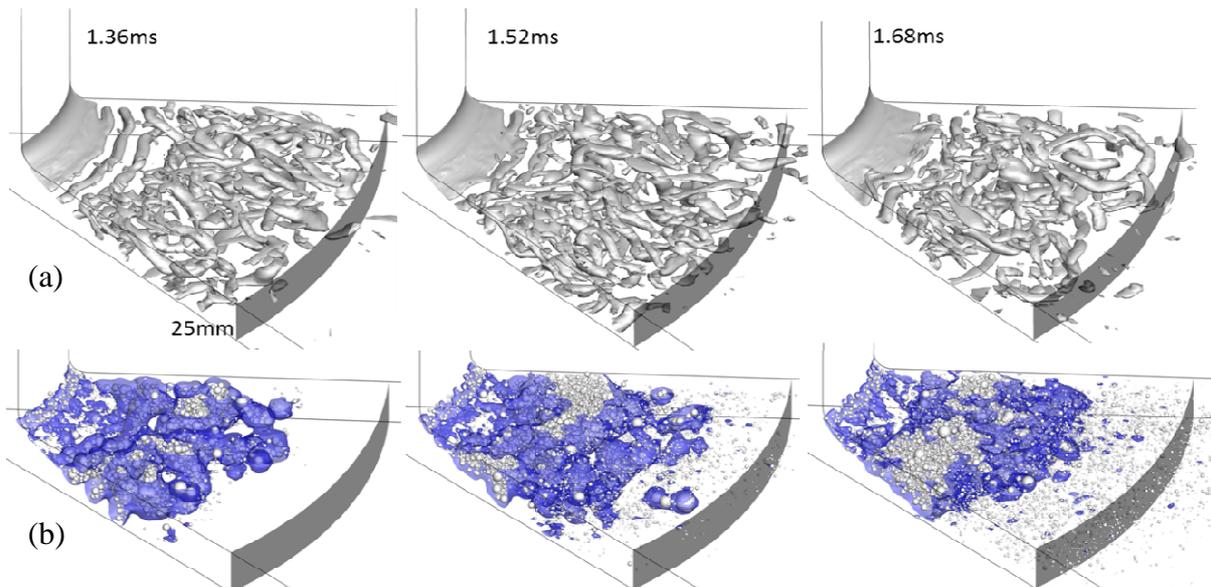
Furthermore, the CFD results provide an indication of the driving mechanism of the cavity shedding. Indeed, as shown in Fig. 9, the mechanism of the cavity detachment seems to be the re-entrant jet formed between the cavity and the adjacent wall. To be more specific, the cavities formed at the primary inception point at the turn are unstable, thus at some point, a re-entrant jet is formed, starting from the cavity closure location, which forces the cavity to separate from the wall. During the cavity separation, significant vorticity is generated due to the opposing directions of the bulk of the flow and the re-entrant jet. Afterwards, the cavity travels downstream while it may grow further, due to the influence of vorticity. Analysis of the flow field using sampling probe points and performing FFT shows frequencies beginning from 2500Hz till 25000Hz.



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Fig. 9. Detailed view during the detachment of a vapour cavity. The effect of the re-entrant jet is visible in the zoomed in region. The contour denotes the vapour fraction and the dashed line denotes the radius of 25mm.

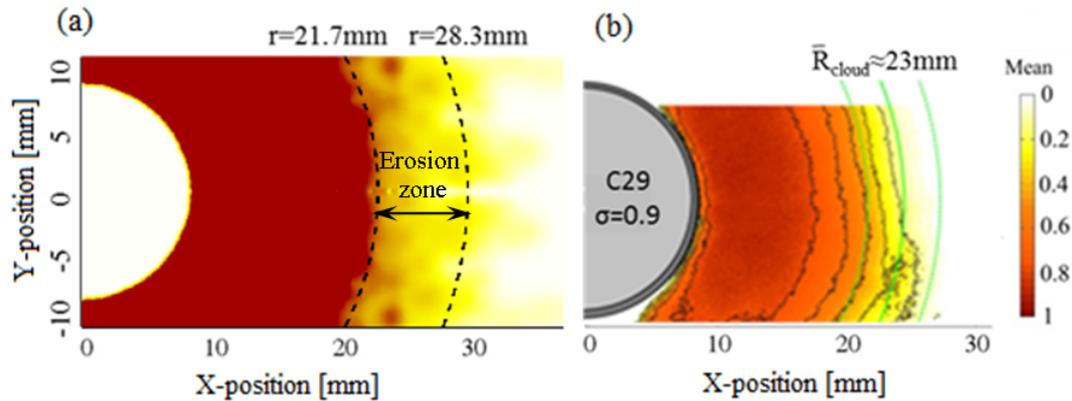
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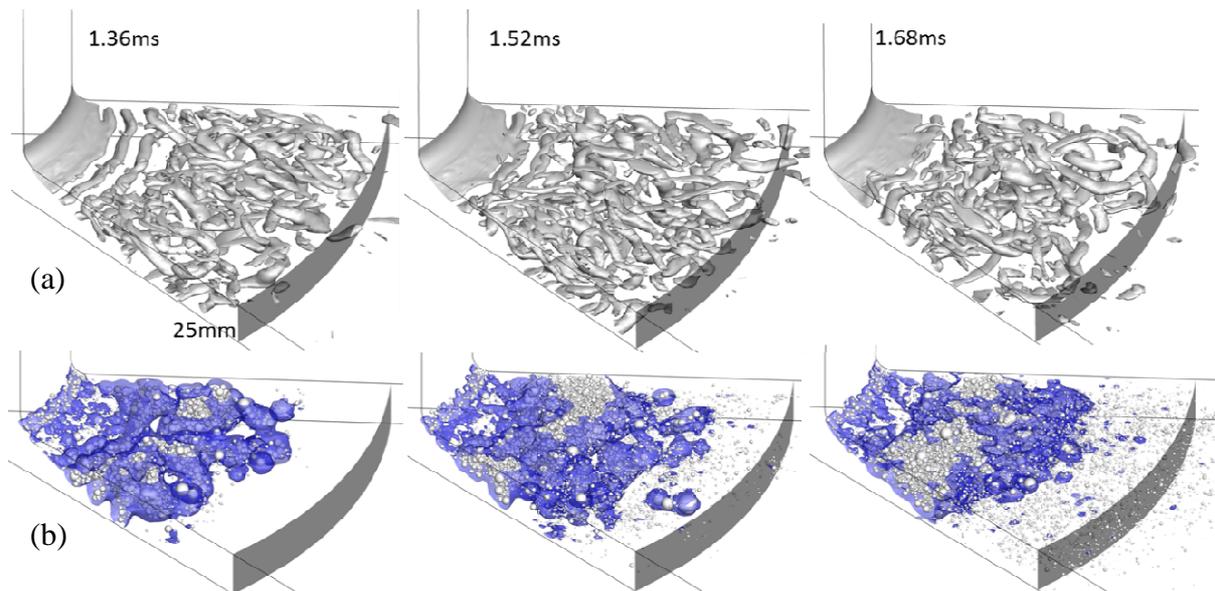
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Fig. 10a, the vortical structures formed due to the flow direction change are shown. For the representation, the second invariant of the velocity vector was used [36]. From the results, it is found

399 that vortex tubes are formed after the sharp turn, organizing in filament-like structures (similar
 400 structures are found from the experimental results as well, e.g. at Fig. 2 at 0.506-0.545ms at the
 401 vicinity of the nozzle exit), which are convected by the flow and, later on, merge into more
 402 complicated structures. Pressure at the vortex cores may drop below the saturation pressure, thus
 403 forming moving cavitation inception sites. Eventually, vortices are dissipated due to the fluid
 404 viscosity, resulting to the collapse of vapour structures. The corresponding plots for the cavitation
 405 bubbles utilised and the resulting vapour volume fraction iso-surface of 0.5 is indicated in Fig. 10b.
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 408 Comparison of those results against the images of the previous Fig. 2, is shown in

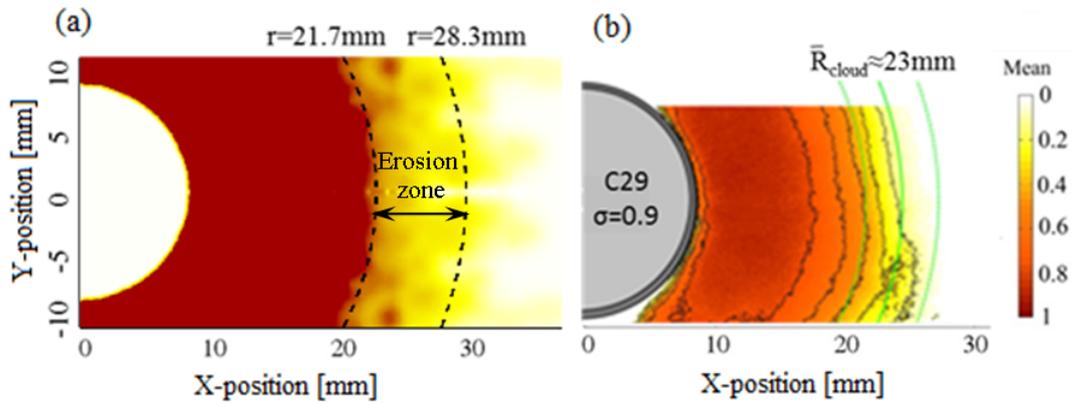


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 410 Fig. 11 ($\sigma=0.9$ and $P_{\text{down}}=19\text{bar}$) where the time averaged probability of vapour presence is shown for
 411 both the experiment and the hybrid RANS/LES results, projected on the lower disk; the probability
 412 was estimated based on a threshold value which was 5% vapour fraction for the CFD calculations
 413 (i.e. if the average vapour fraction at the line of sight is more than 5%, then the probability is 1, else it
 414 is zero). The comparison indicates similar locations of bubble cloud formation and collapse regions,
 415 e.g. the vapour structures begin to collapse at $\sim 20\text{mm}$ from the axis of symmetry (see Fig. 10) and
 416 may disappear just after the 25mm. Regarding the vapour distribution in the normal direction between
 417 the two disks no experimental data are available. However, on average, the vapour distribution from
 418 the CFD results shows a stronger vapour presence near the upper disk and this could possibly
 419 correlate to the extended erosion zone found at the specific disk.
 420



421

422 **Fig. 10:** (a) Vortical structures, indicated with the second invariant of the velocity gradient tensor and
 423 (b) representative bubble parcels utilized for the simulation of cavitation; the blue iso-surface
 424 corresponds to cavitation volume fraction of 0.5. The simulation conditions correspond to C29, with
 425 $\sigma \approx 0.9$ and $P_{\text{down}} = 19 \text{ bar}$.



426 **Fig. 11.** (a) Time averaged vapour probability distribution from the CFD calculations, for case to C29,
 427 with $\sigma \sim 0.9$ and $P_{\text{down}} = 19 \text{ bar}$. The dashed lines represent the area of erosion of the lower disk for the
 428 specified cavitation number. The region of erosion coincides well with the collapse of the vapour
 429 structures. (b) The average experimental vapour probability distribution.

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432

5. Spatial mean cavitation distribution and cloud length

434 Having described the flow development we now proceed to the presentation of the results obtained
 435 from the post-processing of the collected images. The first series of results is presented in Fig. 12. It
 436 shows the spatial distribution of the temporal mean cavitation presence and its standard deviation for
 437 selected operating conditions of Table 1. In each plot, the feed inlet area corresponds to the circle in
 438 the middle of the picture. As mentioned earlier, concentrically with it, a thin zone has been plotted
 439 without any value. This was because in the area of inlet, light reflections have prevented the collection
 440 of clear images and, thus, the cavitation could not be distinguished automatically.

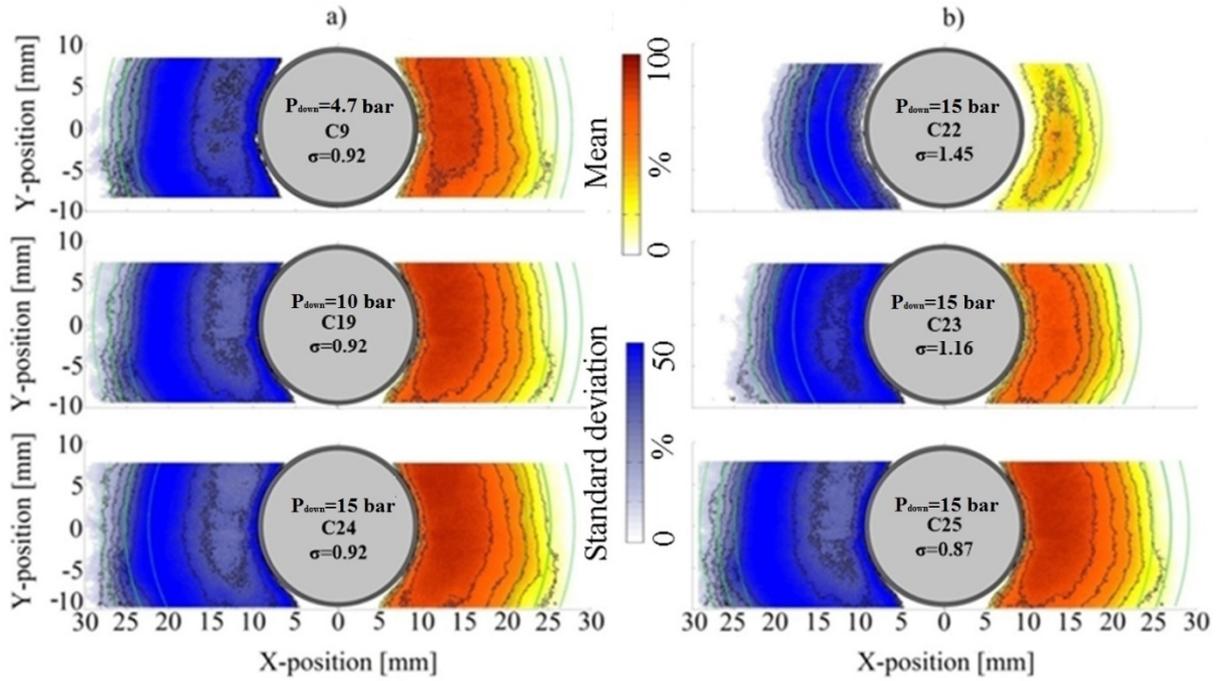
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442 A general remark from Fig. 12 is that there is a slight asymmetry in the time averaged results. This is
 443 believed to be caused by the asymmetry induced by the outlet pipes. As shown in Fig. 1a, the
 444 geometry of the device is not entirely axisymmetric at the outlet of the disks gap; there are four outlet
 445 pipes that are positioned every 90 degrees. These pipes probably induce a disturbance in the velocity
 446 field, imposing a direction of preference, which is manifesting at the lower part of the spatial
 447 distributions in Fig. 12, for a X-position of $\sim 25 \text{ mm}$. For the time being, it is not possible to quantify
 448 the exact effect of the outlet pipes or upstream effects (pipe bends) in the induced asymmetry of the
 449 flow field.

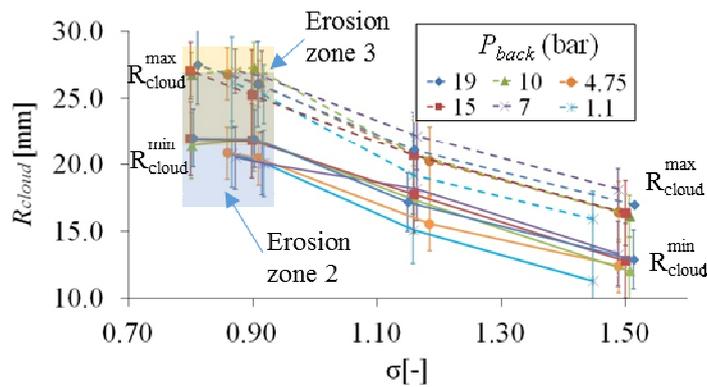
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451 The effect of cavitation number, σ , can be realised from Fig. 12b. This parameter has an appreciable
 452 effect on the extent of cavitation. For high cavitation numbers, mean values have a maximum of less
 453 than 50%, which implies that most of the running time no cavitation is present. With decreasing σ ,
 454 both the appearance becomes more frequent and the cloud propagates further into the flow. For
 455 sufficient enough pressure difference, the cloud reaches a 'steady-state' condition and it does not
 456 extend further in the radial direction. The erosion sites 2 and 3, as shown in the previous Fig. 1b
 457 coincide well with the estimated cloud length, which effectively indicates the area where the
 458 cavitation cloud collapses. This zone coincides well with the area of high standard deviation values.
 459 Effectively, this area is exposed to successive cloud collapse events. Fig. 12a presents the same
 460 parameters but this time the cavitation number has been kept constant and the back pressure is
 461 changing. It is clear that changing the back pressure has only marginal effect of the cavitation
 462 development when σ is kept constant. The cloud length is indicated with the solid green line while the
 463 corresponding standard deviation is indicated with the green dotted lines residing to the left and right

464 of the solid one. The estimated cloud length values are also shown on Fig. 13a as function of the
 465 cavitation number for all back pressure conditions investigated; the standard deviation is also
 466 indicated with the vertical bars for all operating points. A clear trend is observed: the cloud length
 467 decreases linearly with σ , while there are no significant variations with back pressure.
 468



469
 470 **Fig. 12:** Spatial distribution of the mean (time averaged) and its standard deviation (expressed as % of
 471 the mean) of cavitation presence in the visualised area. The green solid line indicates the temporally
 472 mean cloud length and the green dotted lines indicate its standard deviation. (a) Effect of back
 473 pressure for fixed cavitation number (cases C9, C19, C24). (b) Effect of cavitation number for fixed
 474 back pressure (cases C22, C23, C25 of Table 1).
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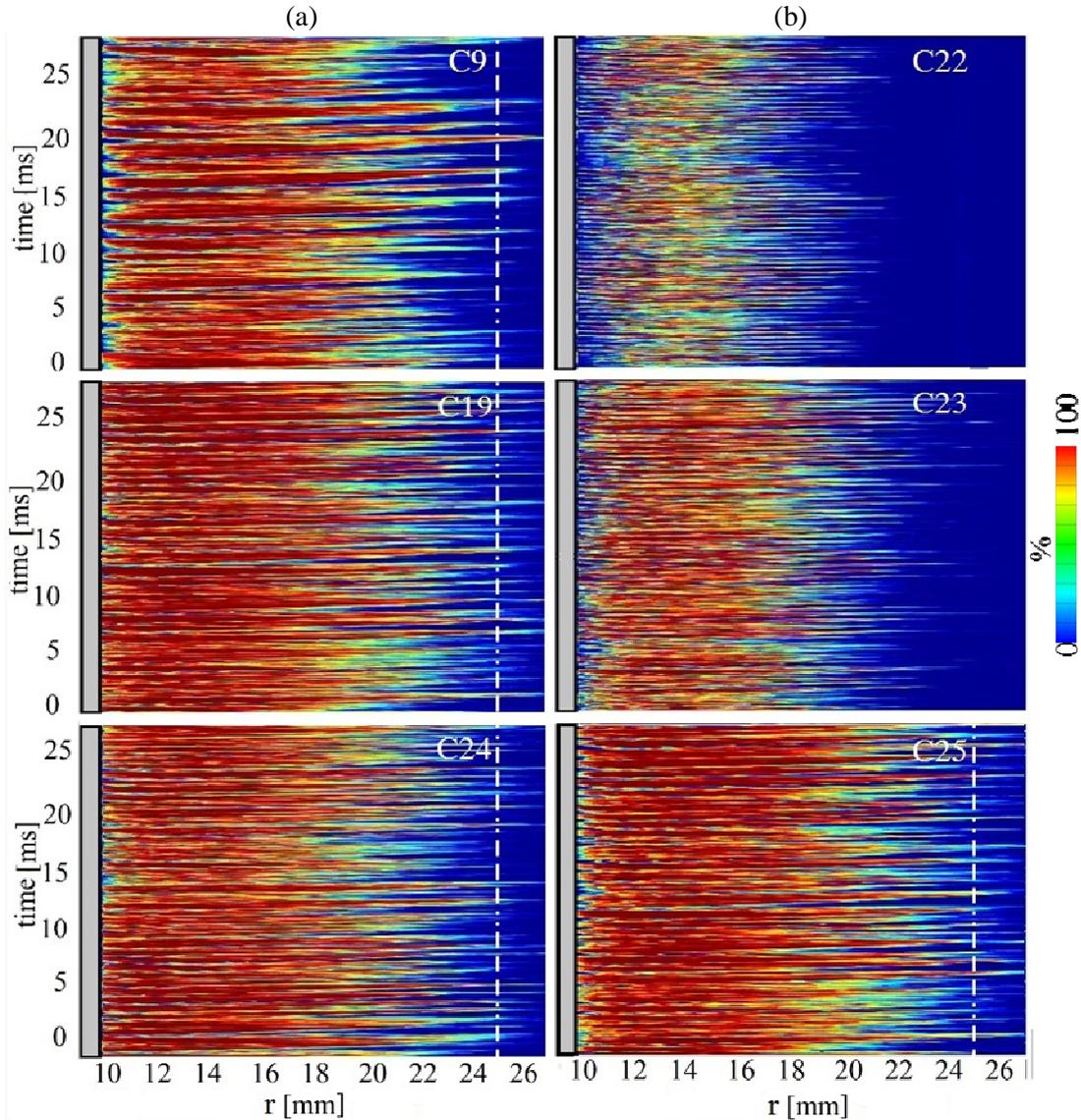


476
 477 **Fig. 13:** Maximum (dashed lines) and minimum (solid lines) cavitation cloud length as function of
 478 cavitation number σ for different downstream pressures; the extent of the erosion zones 2 and 3 for a
 479 cavitation number of ~ 0.9 (see Fig 1) are also superimposed.
 480

481 6. Temporal development of cavitation cloud and shedding frequency at location of collapse

482
 483 Having described the development of cavitation and its mean distribution, we proceed now to
 484 presentation of results revealing more information about its temporal development. In particular,
 485 results obtained by utilising the averaging procedures along the circumferential direction, as described
 486 earlier, are presented in Fig. 14. The corresponding temporal variation of this mean value is plotted as

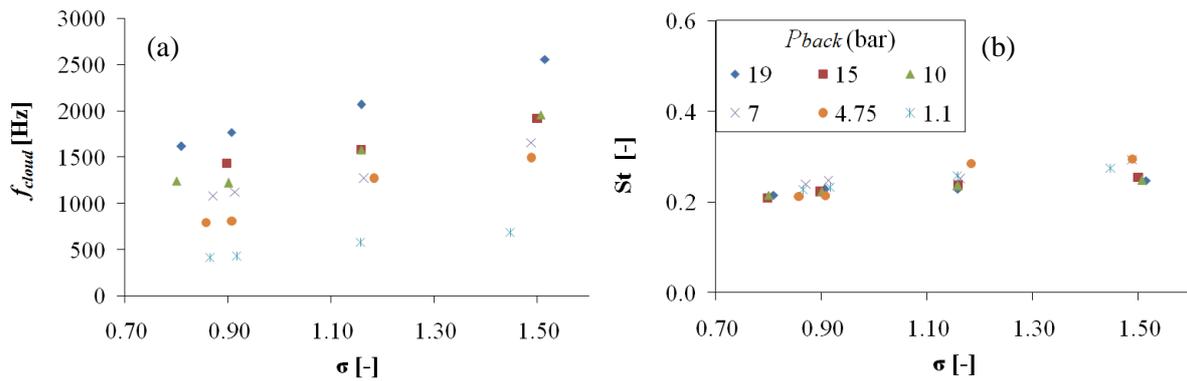
487 function of the radial distance from the inlet. The conditions of Fig. 14a correspond to the same
 488 cavitation number $\sigma=0.92$ (cases C9, C19 and C24 of Table 1) while plots of Fig. 14b correspond to
 489 conditions where the cavitation number is changing and the back pressure has been kept constant
 490 (cases C22, C23 and C25 of Table 1).
 491



492 **Fig. 14:** Temporal variation of the circumferentially mean cavitation presence as function of the
 493 distance from the axis of symmetry. (a) Effect of back pressure for constant σ (cases C9, C19 and C24
 494 of Table 1) and (b) effect of σ for constant back pressure (cases C22, C23 and C25 of Table 1). The
 495 vertical dotted while line indicates the mean erosion position of 25mm, visible only in cases where the
 496 cavitation number is ~ 0.9 .
 497
 498

499 From these plots, it is possible to evaluate the frequency of the cloud appearance/disappearance and
 500 collapse. In particular, it is of interest to estimate the main cloud frequency, f_{cloud} , at the distance of
 501 25mm which corresponds to the erosion sites 2 and 3 and the corresponding Strouhal number. The
 502 f_{cloud} has been evaluated by the fast Fourier transformation (FFT) and it is shown in Fig. 15a for all
 503 operating conditions tested. It becomes apparent that CFD predictions of the flow field frequency is
 504 higher than that of the experimental shedding frequency. However, direct comparison of the temporal
 505 frequencies between the experiment and CFD is not straightforward, since the flow field was not

506 obtained from the experiment; experimental frequencies were calculated based on the macroscopic
 507 flow features, without taking into account the intricate temporal fluctuations of the flow field. Similar
 508 to past observations of cavitation cloud shedding (for example, [18]) the clouds at high σ are small
 509 and detach/collapse frequently, whereas at low σ the clouds grow and collapse at a slower rate. The
 510 f_{cloud} increases with increasing downstream pressure, due to increase of the flow velocity. This
 511 frequency of collapse at the distance of R_{cloud} as plotted here is similar to the frequency of formation
 512 of the ‘large scale’ clouds as estimated earlier from the raw images of Fig. 2. Finally, Fig. 15b shows
 513 the Strouhal number, estimates using as length scale the cloud length and the mean velocity of the
 514 flow at this location. It is noticeable that the Strouhal number seems to be relatively constant for all
 515 tested conditions.
 516



517 **Fig. 15:**(a) Cloud collapse frequency (f_{cloud}) at 25mm from the axis of symmetry, as function of σ for
 518 different downstream pressures (P_{down}). The main frequency has been evaluated utilizing the power
 519 spectral density criterion [37]. (b) Strouhal number estimated using the f_{cloud} , the disk distance
 520 (2.5mm) and the corresponding mean flow velocity at a radius of 25mm.
 521
 522

524 7. DISCUSSION OF RESULTS

526 Both experimental and computational results show an intricate flow field occurring inside the device;
 527 indeed, the flow is highly unsteady showing a periodic behaviour which varies depending on the
 528 cavitation number, σ , and Reynolds number, Re . At high cavitation numbers cavitation is not well
 529 defined, that is no coherent cavitation structures are formed. As cavitation number decreases, the
 530 cavitation influence becomes more significant; cavitation becomes more intense and extends at a
 531 larger area, from the nozzle exit to a maximum radial distance of almost 30mm (see Fig. 14). The
 532 effect of Reynolds number is primarily linked to the shedding frequency of the cavitation structures;
 533 indeed, when considering a constant cavitation number σ , at low back pressures (which also
 534 corresponds to low Reynolds number) the shedding frequency is lower. On the other hand, as the
 535 downstream pressure is increased, for constant cavitation number σ , the frequency of the shedding
 536 also increases.
 537

538 When considering a constant downstream pressure, decrease of the cavitation number results to a
 539 lengthened and more regular cavity which detaches at lower frequency, while increase of the
 540 cavitation number results to smaller and more unstable cavities forming and collapsing at higher
 541 frequencies. While this looks counterintuitive, since the decrease of the cavitation number results to
 542 increased Reynolds number and, theoretically, to a higher frequency, it is justified by the fact that at
 543 low cavitation numbers cavitation structures live longer thus have the time to form agglomerations. In
 544 that case, individual vortex cavities are impossible to distinguish, giving the impression of a lower

545 shedding frequency. Contrary, at higher cavitation numbers at similar Reynolds (thus at higher
546 downstream pressures), cavities tend to remain separate, thus the apparent frequency seems higher.

547

548 The dependence of the Reynolds number on the frequency is justified by the increased vorticity that is
549 being generated downstream the turn. As it was shown from numerical results, the shear layer that
550 forms downstream is unstable and generates significant vorticity. The increase of the Reynolds
551 number with the corresponding increase of the velocity increases the rate of generation of vortices and
552 consequently the frequency of shedding of the resulting cavitating structures.

553

554 A complementary explanation of the unsteadiness of the cavitation shedding process, supported by
555 CFD results, is the influence of the re-entrant jet, formed at the vicinity of the cavity closure; the re-
556 entrant jet has been identified also in the literature as a feature driving the flow unsteadiness for both
557 internal and external flows, e.g. [38, 39]. The distinct phases of the cavity growth and detachment are
558 described below(also shown schematically in Fig. 16);

559 1) Initially cavitation forms at the turn (primary inception site, see also the description in CFD
560 simulations section), due to the rapid acceleration of the liquid.

561 2) The cavity stretches over time due to the local flow conditions, i.e. the shear and the drag,
562 displacing liquid.

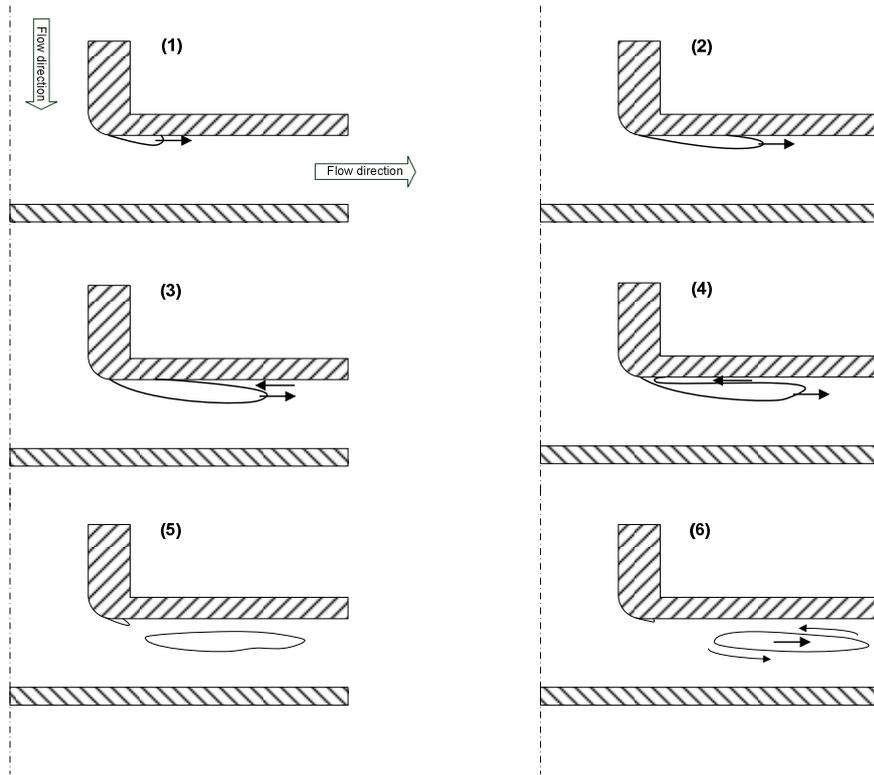
563 3) The closure of the cavity is a saddle point [40], thus its location is highly unsteady. A re-entrant jet
564 is formed, which pushes the closure point back towards the turn. The cavity begins to separate from
565 the adjacent wall.

566 4) The re-entrant jet detaches the cavity from the wall, while impinging on the primary inception site.

567 5) The cavity is entirely detached from the primary inception site and the rear part transforms into a
568 bubble cloud. Around the cloud there is significant vorticity, due to the momentum of the re-entrant
569 jet, which is in the opposite direction of the main flow. Moreover, the primary inception site starts to
570 collapse, thus causing erosion at the vicinity of the turn (erosion zone 2).

571 6) The detached cavity transforms into a bubble cloud and moves downstream following the flow. It
572 rapidly rotates due to aforementioned circulation, thus its pressure may fall below saturation and
573 continue to grow, acting as the secondary inception site. The cycle is repeated from (1).

574



575
 576 **Fig. 16.** The cavity shedding cycle: (1) a cavity is formed at the nearby region of the turn, (2) the
 577 cavity extends due to shear with the surrounding fluid, (3) the elongation of the cavity stops, while a
 578 re-entrant jet is formed, (4) the re-entrant jet detaches the cavity from the adjacent wall, (5) the vapour
 579 cavity is entirely detached from the parent cavity at the turn, (6) the detached vapour cavity follows
 580 the flow and travels downstream, while it may expand even more due to vorticity.
 581

582 The growth and collapse of the vapour clouds is speculated to be linked to the compressibility
 583 effects that occur in cavitating flows. Indeed, it is known that the bubbly mixture of
 584 vapour/liquid is highly compressible. As mentioned above, a series of vapour cavities is shed
 585 from the primary inception site at the turn. These vapour cavities form collectively the bubble
 586 cloud, as shown in Fig. 2. As the bubble cloud is travelling downstream, pressure is recovering and
 587 vorticity is dissipating due to viscosity. Once the surrounding pressure force counteracts the vorticity
 588 induced centrifugal force, the edge of the bubble cloud, approximately at a radial distance of 25mm
 589 from the axis of symmetry, starts to collapse. The collapsing bubble cloud may cause a cascade of
 590 pressure waves, due to the rapid deceleration of the surrounding water, which could contribute to the
 591 erosion in zones 1 and 3.
 592

593 8. CONCLUSIONS

594
 595 Visualization and CFD results of the cavitation cloud developing inside a hydraulic device have been
 596 presented, providing more insight into the details of the sheet/cloud cavitation development for the
 597 flow conditions where previous data on material's response to cavitation erosion have been
 598 recorded[1]. As shown from the visualization experiment, the dynamics of the cavitation clouds are
 599 complex. In all cases examined, the cloud is generated in the vicinity of the outlet of the feed nozzle.
 600 Then the cavitation cloud grows up and is convected by the flow, until it reaches a maximum distance,
 601 which varies over time. Afterwards, the cloud collapse is followed by successive formation of clouds.
 602 The erosion zones coincide with the areas corresponding to the maximum and minimum cloud length.
 603

604 Despite the axisymmetric geometry utilized, instantaneous pictures of cavitation indicate variations in
 605 the circumferential direction. A slight deviation from axis-symmetry is found in averaged results too,

606 which is attributed to the outlet piping of the device, which is not axis-symmetric. Image post-
607 processing has been used to characterize in more detail the phenomenon. In particular, the mean
608 cavitation appearance and the cavity length have been estimated, showing good correlation with the
609 erosion zone. This also coincides with the locations of the maximum values of the standard deviation
610 of cavitation presence. Cloud collapse length was estimated with an uncertainty of less than 10% and
611 it was found to decrease fairly linearly with cavitation number. In addition, the dominant frequency of
612 the ‘large-scale’ cavitation clouds has been estimated through FFT. Cloud collapse frequencies vary
613 almost linearly between 200 to 2000Hz as function of the cavitation number and the downstream
614 pressure but the corresponding Strouhal number remains almost constant for all conditions. It is
615 speculated that pressure wave propagation affects the cavity shedding mechanism, creating the gaps
616 in-between subsequent cavitation clouds.

617
618 The main correlations between the cavity length and shedding frequency with the downstream
619 pressure and cavitation number are:

620 - The increase of the cavitation number gives smaller cavitation zones. At very high cavitation
621 number, cavitation occurrence is sparse and in-coherent. On the other hand, decrease of the cavitation
622 number leads to more coherent cavitation structures, extending at larger areas, from 9mm till almost
623 30mm. The cavitation number is the sole factor affecting the maximum extent of the cavity.

624 - The increase of the downstream pressure, for the same cavitation number, leads to an increase in the
625 shedding frequency. This is due to the increase of the Reynolds number, which enhances turbulence
626 and vortex shedding.

627 - The decrease of the cavitation number for a constant downstream pressure gives a reduction of the
628 shedding frequency. This is explained by the fact that, at low cavitation numbers, individual cavitation
629 vortices live longer and form agglomerates that are difficult to distinguish, thus giving the impression
630 of a lower apparent shedding frequency.

631
632 From the CFD results, it becomes apparent that a mechanism similar to vortex shedding occurs.
633 Indeed, significant vorticity is generated downstream the turn, organizing in vortex tubes and
634 manifesting as filament-like structures. This was confirmed by the experimental observations, since
635 similar thread like structures have been captured during the image acquisition process. There is
636 indication that pressure inside the vortex cores may drop well below the saturation pressure, resulting
637 to cavitation inception downstream the turn. The LES/RANS methodology used in the present work
638 shows that there could be a secondary nucleation site downstream the turn; this site cannot be
639 predicted by pure RANS methodologies but, at the present, cannot be confirmed by experimental
640 observations, thus requiring further examination. However, it is noticeable that the erosion free zone,
641 located in-between two erosion zones, coincides with the areas where CFD predictions indicated as
642 the secondary cavitation inception site. The contribution of the pressure wave propagation within the
643 bubbly medium is possibly a driving factor on the development of discrete cavitation clouds, but in
644 the present cannot be taken into account, due to limitations of the modelling capabilities of the
645 software used.

646
647

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