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Neural-Network Based Vector Control of VSC-HVDC Transmission Systems

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Abstract—The application of high-voltage dc (HVDC) using voltage-source converters (VSC) has surged recently in electric power transmission and distribution systems. An optimal vector control of a VSC-HVDC system which uses an artificial neural network to implement an approximate dynamic programming algorithm and is trained with Levenberg-Marquardt is introduced in this paper. The proposed neural network vector control algorithm is analyzed in comparison with standard vector control methods for various HVDC control requirements, including dc voltage, active and reactive power control, and ac system voltage support. Assessment of the resulting closed-loop control shows that the neural network vector control approach has superior performance and works efficiently within and beyond the constraints of the HVDC system, for instance, converter rated power and saturation of PWM modulation.

Keywords—VSC-HVDC transmission and distribution; renewable energies; neural network; adaptive dynamic programming; Levenberg-Marquardt, voltage-source converter

I. INTRODUCTION

VSC-HVDC relies on voltage source converters (VSCs) and insulated gate bipolar transistors (IGBT) [1] for the transmission and distribution of energy. VSC-HVDC shows distinct advantages, namely: low cost, small environmental footprint, easy integration of renewables to the transmission grid, and high transmission stability and power quality [2].

Since HVDC transmission using VSC was first installed in 1997 in Gotland (Sweden) [3], two main manufacturers refer to the technology of HVDC transmission using VSCs, namely, ABB under the name of HVDC Light [3], with a power rating from tenths of megawatts up to over 1000 MW, and Siemens under the name of HVDC Plus ("Plus" - Power Link Universal Systems) [4]. VSC-HVDC technology has been broadly applied

in microgrids and in integration of solar and offshore wind into the power transmission system [5, 6].

Typically, a VSC-HVDC system is controlled via a nested-loop control, which in turn is built on standard vector control methods [5-7]. However, recent studies show that a complete decoupled vector control cannot be achieved using conventional methods, which affects the performance of the standard vector control method, particularly if a converter works beyond the PWM (pulse-width-modulation) saturation bound [8].

It has also been indicated that there are unresolved challenges which prevented effective integration of offshore wind to the grid using HVDC [9]. It has been shown, on the other hand, that an optimal vector control of a grid-connected converter can be approximated by using an artificial neural network [10].

In this paper, a neural network control technique based on approximate dynamic programming principles which meets various HVDC control requirements is presented. The paper makes the following new contributions:

- 1) a neural network control strategy for VSC-HVDC systems
- 2) neural network design and training that can handle VSC-HVDC control requirements properly under physical system constraints, and
- 3) comparison of standard and neural network control methods for power control and management of a HVDC transmission system.

With this aim in mind, we first specify the configuration of a VSC-HVDC system in the next section. Section III shows both the standard and a novel neural network vector control topologies for HVDC inverter and rectifier stations. The training of the neural network vector controller is discussed in Section IV. Performance of a VSC-HVDC system by using the conventional and neural network vector control methods is discussed in Sections V for different HVDC operating conditions. We shall finish with conclusions.

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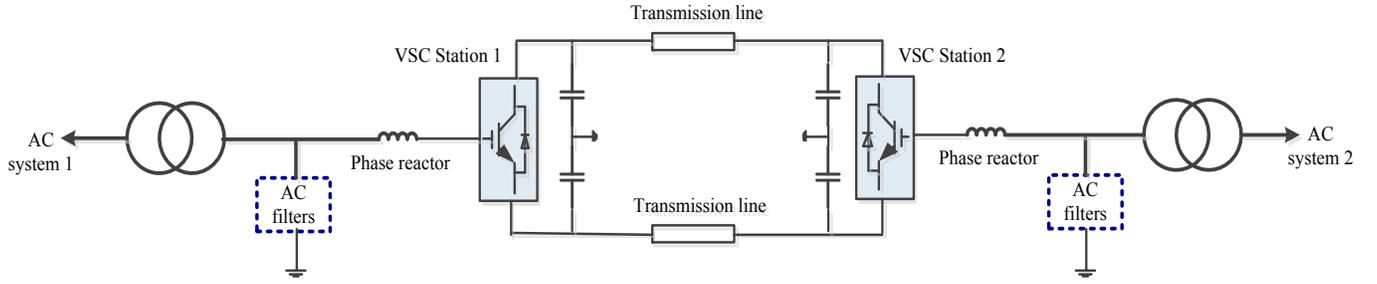


Fig. 1. Configuration of a two-terminal VSC-HVDC transmission system

II. CONTROL OF VSC-HVDC SYSTEM

A. VSC-HVDC Transmission

Transmission in VSC-HVDC involves VSC-based converter stations and a high-voltage dc transmission system [5, 6].

The stations need to efficiently regulate their reactive power or ac system voltage support control and their active power or dc system voltage control [11]. While each of the converter stations controls its reactive power independently, the active power entering the HVDC system must be equal to the resultant active power leaving it [12].

In the HVDC system, one station is built to control the voltage of the dc system where as the other VSC stations control the active power.

Figure 1 shows a schematic a VSC-HVDC system with two stations. The stations are connected to an ac system via a phase reactor and a transformer. An ac filter is used on each side of the ac system to reduce or eliminate the harmonics entering the ac systems. Regarding dc, the stations are connected to a capacitor bank. Stations work as a rectifier and an inverter respectively.

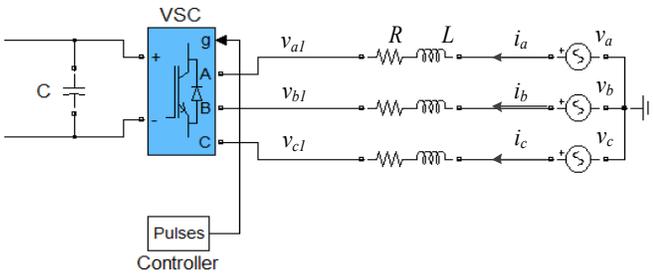


Fig. 2. Design of a VSC station

B. VSC Station Model in d-q

Figure 2 details how a VSC station is connected to an ac system, in which a capacitor is connected across the dc side of the VSC, the composition of a resistor R and an inductor L represents the phase reactor, and a three-phase voltage source stands for the voltage at the Point of Common Coupling (PCC). In the d-q reference frame [7, 8], the VSC-HVDC system is represented by

$$\frac{d}{dt} \begin{bmatrix} i_d \\ i_q \end{bmatrix} = - \begin{bmatrix} R/L & -\omega_s \\ \omega_s & R/L \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} - \frac{1}{L} \begin{bmatrix} v_{d1} \\ v_{q1} \end{bmatrix} + \frac{1}{L} \begin{bmatrix} v_d \\ v_q \end{bmatrix} \quad (1)$$

where ω_s is the angular frequency of the ac system voltages and the rest of the symbols in Eq. (1) are consistent with those indicated in Fig. 2, e.g., $v_a, v_b, v_c \leftrightarrow v_d, v_q$; $i_a, i_b, i_c \leftrightarrow i_d, i_q$; and $v_{a1}, v_{b1}, v_{c1} \leftrightarrow v_{d1}, v_{q1}$.

C. Vector Control of VSC Stations

The general VSC vector control method deploys a nested-loop structure with inner and outer current loops, the former being faster than the latter, as shown in Fig. 3 [5, 13]. Active power or dc voltage is controlled through the d-axis loop, whereas, the q-axis loop controls the reactive power or PCC voltage.

The power controllers generate d- and q-axis references to the inner current-loop controller where as the inner controller applies a three-phase sinusoidal voltage signal directly to the VSC converter [5].

The overall strategy for the conversion of d-q signals into three-phase sinusoidal signals is illustrated in Fig. 3, in which v_{d1}^* and v_{q1}^* are d- and q-axis output voltages.

The d- and q-axis voltages are transformed to the three-phase sinusoidal voltage signals, v_{a1}^* , v_{b1}^* and v_{c1}^* , through Park transformation [8].

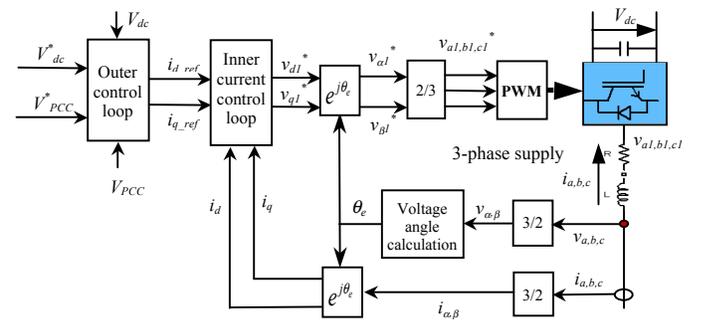


Fig. 3. Common vector control structure of HVDC VSC

each time step k in Eq. (9), where \vec{i}_{dq} represents actual dq current vector of ac system, and \vec{e}_{dq} and \vec{s}_{dq} represent error current and integral of the error current as shown in Fig. 5. The integral term can help to remove the steady error and to maintain the stable operation of the converter when the converter has a potential to go over the PWM saturation limit. This is analyzed in Section V-B.

IV. DETERMINE CONTROLLER PARAMETERS

A. Tuning PI Parameters of Standard Vector Controller

The tuning of the conventional current-loop PI controller is based on Fig. 6. Here, the PI block stands for a d- or q-axis loop current controller, and $1/(L \cdot s + R)$ represents the plant transfer function for a d- or q-axis current loop (Eqs. (2) and (3)) [8, 19, 20]. k_{FB_I} is the gain of the feedback path, for example, then gain of a current sensor; and k_{PWM} is the gain of the power electronic converter. Based on Fig. 6, the best possible gain of the PI controller can be tuned conveniently with Matlab Simulink. However, there are only two parameters that can be tuned for each PI controller.

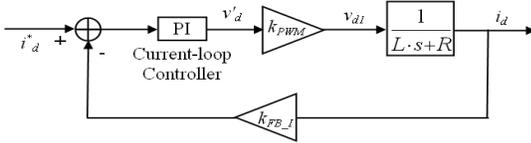


Fig. 6. A system block diagram for design of current-loop PI controller

B. Training Neural Network Vector Controller

The neural-network vector controller was trained using dynamic programming (DP) principles, aiming to approximate optimal control. DP employs Bellman's Principle of Optimality [21, 22, 23]. The typical structure of a discrete-time DP problem includes a performance index, or cost function, and a discrete-time system mode [23]. The DP cost function which we used for this VSC vector-control problem was defined as:

$$C(\vec{i}_{dq}(j), \vec{w}) = \sum_{k=j}^{\infty} \gamma^{k-j} U(\vec{e}_{dq}(k)), j > 0, 0 < \gamma \leq 1 \quad (10)$$

where γ is a constant referred to as the discount factor, and U is defined as:

$$U(\vec{e}_{dq}(k)) = \left[e_d^2(k) + e_q^2(k) \right]^\alpha \\ = \left\{ \left[i_d(k) - i_{d_ref}(k) \right]^2 + \left[i_q(k) - i_{q_ref}(k) \right]^2 \right\}^\alpha, \alpha > 0 \quad (11)$$

and where α is a constant. The function $C(\cdot)$ is referred to as the cost-to-go function from the given state $\vec{i}_{dq}(j)$ and time step j of the DP problem. The objective of the neural network controller is to track a reference current trajectory in an optimal manner, i.e., to hold the actual state \vec{i}_{dq} near a target state \vec{i}_{dq}^* so that the function $C(\cdot)$ in Eq. (10) is minimized. The

neural network was trained by using Levenberg-Marquardt (LM) [24] to minimize the DP cost $C(\cdot)$. We chose the LM algorithm because it is particularly suited to situations in which the model functions are known and differentiable, and because it is the fastest neural network training algorithm for a moderate number of network parameters. The use of LM requires a modification of the cost function $C(\cdot)$ defined in Eq. (10), as follows: Consider the cost function

$$C = \sum_{k=j}^N \gamma^{k-j} U(\vec{e}_{dq}(k)) \text{ with } \gamma = 1, j = 1, \text{ and } k = 1, K, N. \text{ Then,}$$

we rewrite $C(\cdot)$ as:

$$C = \sum_{k=1}^N U(\vec{e}_{dq}(k)) = \sum_{k=1}^N (V(k))^2 \quad (12)$$

where we define $V(k) = \sqrt{U(\vec{e}_{dq}(k))}$. Now, we can derive the

gradient $\partial C / \partial \vec{w}$ as:

$$\frac{\partial C}{\partial \vec{w}} = \frac{\partial \sum_{k=1}^N (V(k))^2}{\partial \vec{w}} = \sum_{k=1}^N 2V(k) \frac{\partial V(k)}{\partial \vec{w}} = 2J(\vec{w})^T \vec{V} \quad (13)$$

where the Jacobian matrix $J(\vec{w})$ is:

$$J(\vec{w}) = \begin{bmatrix} \frac{\partial V(1)}{\partial w_1} & \dots & \frac{\partial V(1)}{\partial w_M} \\ \vdots & \ddots & \vdots \\ \frac{\partial V(N)}{\partial w_1} & \dots & \frac{\partial V(N)}{\partial w_M} \end{bmatrix}, \vec{V} = \begin{bmatrix} V(1) \\ \vdots \\ V(N) \end{bmatrix} \quad (14)$$

Then, the process of updating the weights using LM [24] for the neural network controller can be expressed as:

$$\Delta \vec{w} = - \left[J(\vec{w})^T J(\vec{w}) + \mu \mathbf{I} \right]^{-1} J(\vec{w})^T \vec{V} \quad (15)$$

The parameter μ was adjusted dynamically during training, so as to ensure that cost function always decreased. In order to increase the speed of computation, the weights update in Eq. (15) was conducted using Cholesky factorization [25]. To train the action network, the system data associated with Eq. (1) such as R , L , v_d , and v_q were specified. Before training, the weights of the neural network were randomized with a Gaussian distribution of mean zero and variance 0.1. The training procedure for the current-loop action network

involved: 1) randomly generating a sample initial state $\vec{i}_{dq}(1)$; 2) unrolling the trajectory of the system from the initial state using (7) to (9); 3) randomly generating a changing sample reference dq current time sequence; 4) training the current-loop neural network using Eq. (15) iteratively, to minimize the cost function given by Eq. (10); and 5) iterating over all of the sample initial states and reference sequences, until a stopping criterion associated with the DP cost was met. The training considered the physical system constraints, rated current and

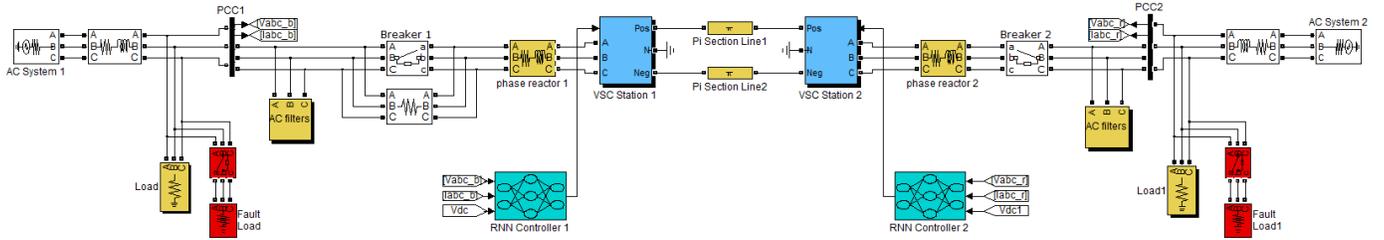


Fig. 7. A VSC-HVDC system with feedback control built in MATLAB SimPowerSystems and RT-LAB

PWM saturation and the impact of variable phase reactor values. This training process resulted in a neural network capable of handling VSC control, under the distorted or imbalanced PCC voltage conditions and short circuits in ac or dc system, as described further in Section V-C.

V. RESULTS

In order to assess the performance of the conventional and neural network methods, we developed a VSC-HVDC system in SimPowerSystems (Fig. 7) (parameters in Appendices). A three-level neutral-point-clamped VSC was adopted in order to guarantee power quality at the stations [26]. Each VSC station includes a phase reactor and ac filters on the ac system side and capacitors, filters and smoothing reactors on the dc system side as shown by Fig. 8. The parameters of a VSC station are given in Table 2. The PI gains of outer-loop controllers and inner current-loop controllers of the conventional method are given in Table 3. Major measurements include voltages, currents, and active and reactive powers at PCC₁ and PCC₂, and dc capacitor voltages.

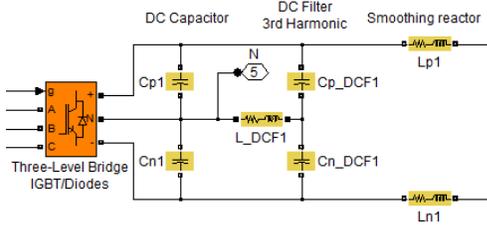


Fig. 8. Components of a VSC station

A. Control of Power Transmission between VSC Stations

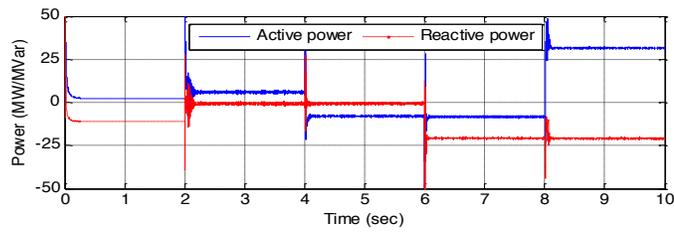
Figures 9 and 10 compare the performance of the HVDC system utilizing both control approaches. At the beginning, the two breakers are in open position and the dc transmission lines are charged to 168kV by ac system 1 through the resistor in parallel with Breaker 1 and the inherent diodes in parallel with the IGBT switches of VSC station 1. After Breaker 1 is closed at $t=2s$, the dc voltage is regulated quickly to 200kV, the reference value, using the neural network vector controller (Fig. 9c) without a high over current (Fig. 9d). At $t=4s$, Breaker 2 is closed and a 20MW is delivered to ac system 1 from ac system 2, which causes the dc system voltage to increase. With the neural network controller, the dc system voltage is quickly stabilized at 200kV. At $t=8s$, the power demand at the VSC-station 2 changes requiring 20MW from ac system 1, resulting in a high dc voltage drop. But, the neural network controller rapidly stabilizes the dc voltage. For

all the other conditions, the neural network controller shows a fast response speed with low current and voltage oscillations. The standard vector controller shows similar performance for power transmission control between the two VSC stations (Fig. 10). Compared to the neural network vector controller, the standard vector controller shows higher oscillations (Figs. 9c and 10c, Figs. 9d and 10d). This is due to the fact that the control action generated by the standard PI controller is determined by the error between the control parameter and the corresponding reference value. Hence, there must be overshoot and settling time issues associated with a PI-based controller. However, the neural network controller is designed and trained based on the DP-based optimal control principle. For an ideal optimal controller, a reference command can be reached immediately without any delay and overshoot. But, this cannot be achieved practically because of physical system constraints. The neural network controller tries to approximate an ideal optimal controller within the physical system constraints. Therefore, the neural network controller has the advantages for fast power transmission control between VSC stations with small oscillations as shown by Figs. 9 and 10.

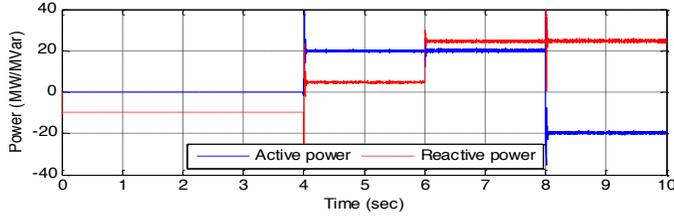
B. Power Transmission and PCC Voltage Control

Now the d-axis loop is employed for active power control while the q-axis loop for PCC voltage control. Figs. 11 and 12 show how the neural network and conventional standard vector controllers perform under normal operating condition; Fig. 13, on the other hand, contrasts the activity of the neural network and conventional controllers under a fault in ac system 1 that appears between 3sec and 7sec. The active power condition is the same as that used in Figs. 9 and 10. For normal operating condition, the neural network and standard controllers perform similarly. However, under the faulted condition, a high reactive power is necessary to rise the PCC voltage, which may cause the converter exceed its PWM saturation limit.

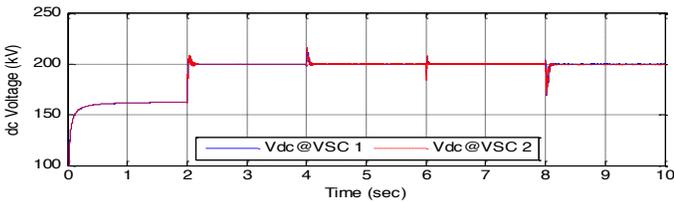
Under the faulted condition, the standard vector controller enters into a malfunction state (Fig. 13d). This is because standard control methods are inherently competing (Section II-A). As a result, when the PWM saturation limit is surpassed, the competing control balance is affected and the control stability of d- and/or q-axis loop could lose. A typical approach to prevent the malfunction of the standard controller is to set a limit on the highest generating reactive power that is allowed. However, the actual real-time reactive power limit is affected by system conditions such as PCC



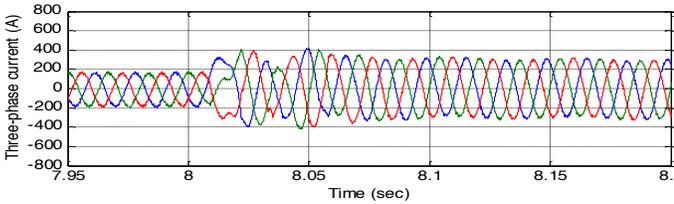
a) Active and reactive power at PCC₁



b) Active and reactive power at PCC₂

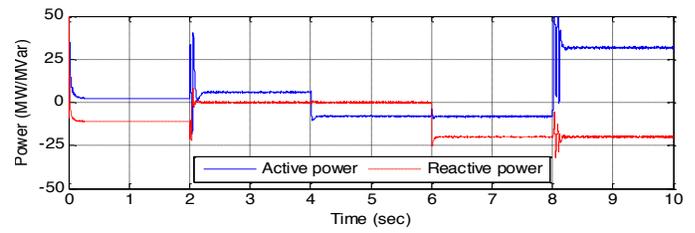


c) dc voltages at VSC₁ and VSC₂

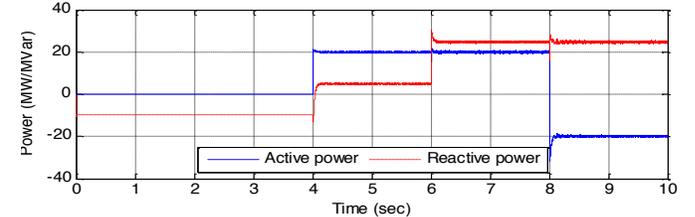


d) Current waveform at PCC₁

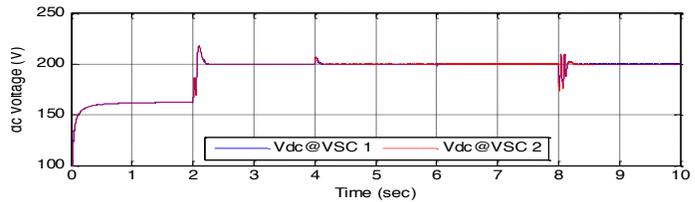
Fig. 9. Neural network control performance



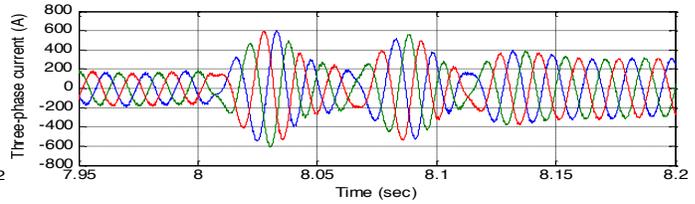
a) Active and reactive power at PCC₁



b) Active and reactive power at PCC₂

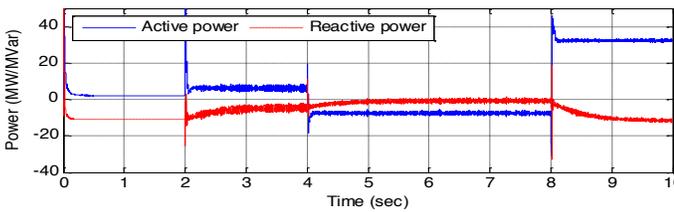


c) dc voltages at VSC₁ and VSC₂ stations

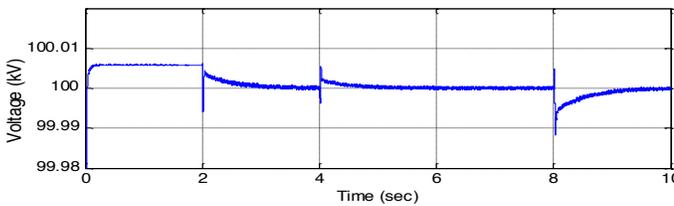


d) Current waveform at PCC₂

Fig. 10. Conventional control performance

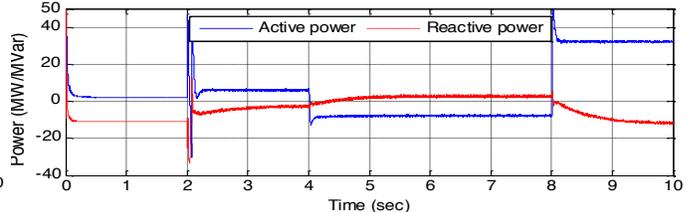


a) Active and reactive power at PCC₁

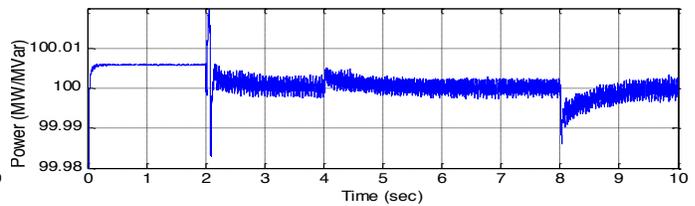


b) Bus voltage at PCC₁

Fig. 11. Neural network control performance



a) Active and reactive power at PCC₁



b) Bus voltage at PCC₂

Fig. 12. Conventional control performance

voltage etc, which causes a challenge to the conventional standard vector controller.

For the neural network controller, the sigmoid function of the network automatically turns the d-axis voltage of the controller into saturation when the PWM saturation appears due to the need of large reactive power. Thus, such power is locked at the maximum generating reactive power according to real-time condition for the highest possible PCC voltage

support control (Fig. 13a) while the control of the active power or dc voltage still keeps the normal control mode (Fig. 13c), which overcomes the challenge of the standard controller and improves VSC-HVDC reliability and stability.

C. Control under Unbalanced Fault

An unbalanced fault is caused by either one-phase or two-phase short circuit in an ac power system. Fig. 14 compares

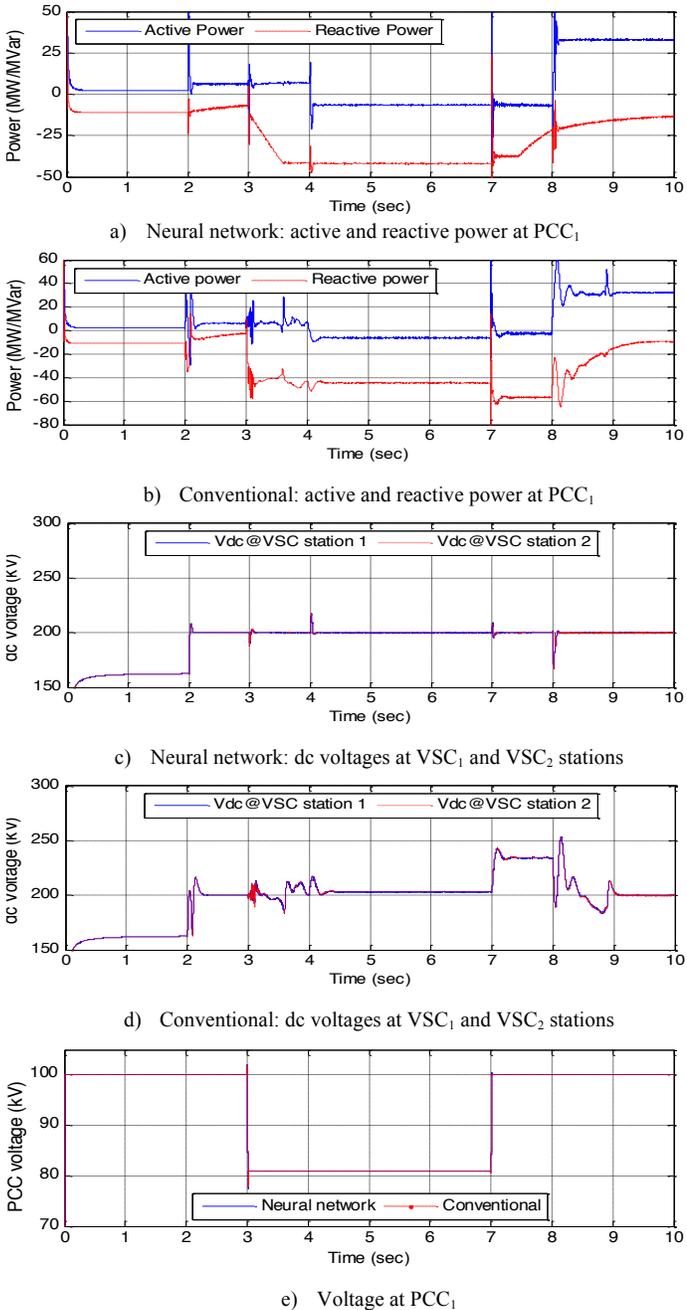


Fig. 13. Performance evaluation under a balanced fault in ac system

the performance of the neural network and standard controllers under a one-phase fault appeared at PCC_1 between 3sec and 7sec. All the other conditions remain the same as those used in Fig. 13. The unbalanced fault made the control of VSC-HVDC more challenging. Both neural network and conventional controllers show oscillation during the fault period. Similar to Fig. 13, the standard controller could lose stability while the neural network controller is stable during the unbalanced fault conditions, demonstrating a good adaptive capability

VI. CONCLUSIONS

In this paper, a neural network vector control mechanism is presented and compared with the standard vector control

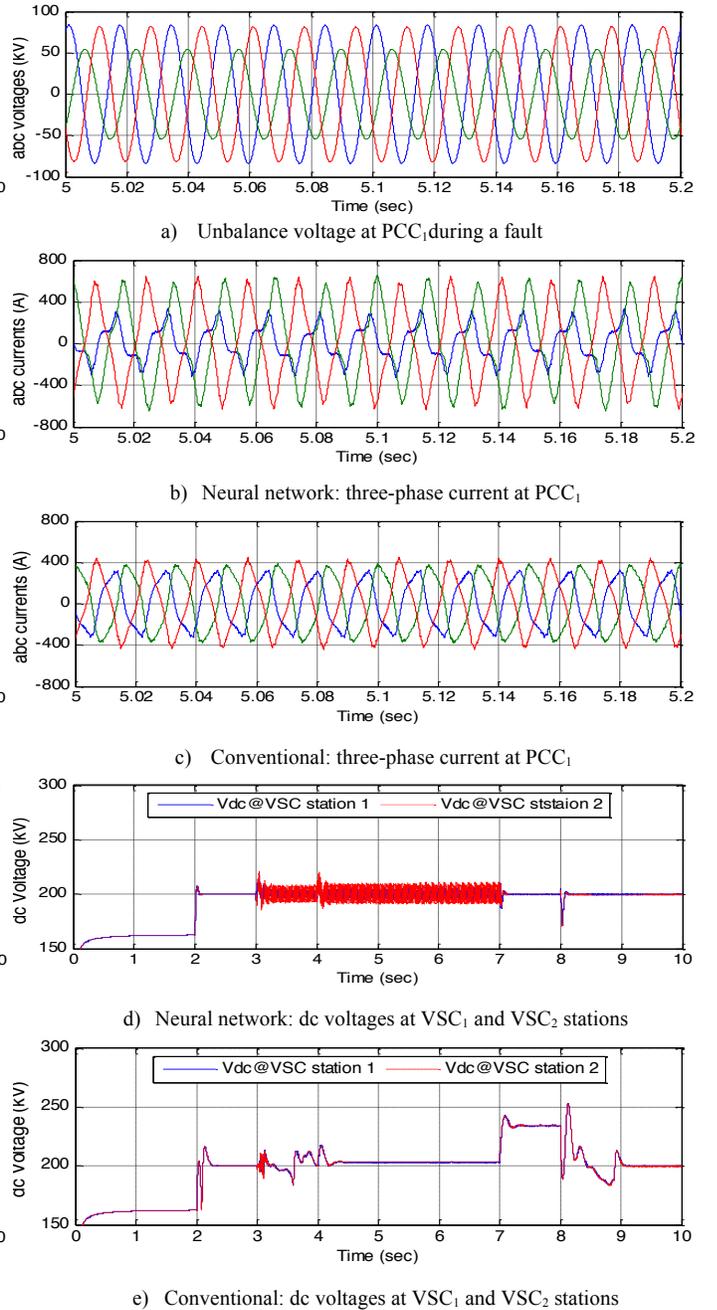


Fig. 14. Performance evaluation under an imbalanced fault in ac system

method for VSC-HVDC control. The neural network controller is trained based on dynamic programming to approximate the optimal control while the standard controller is based on the PI control principle. The neural network controller shows a smaller overshoot and responds faster compared to the conventional controller.

In the PCC voltage support control mode, the conventional standard controller may enter into a malfunction state especially under a high voltage drop at the PCC bus, which may affect the stable operation of the HVDC system. The neural network controller can overcome this limitation by achieving the highest possible PCC voltage support control while the control of the active power or dc voltage is not affected.

For an unbalanced fault in the ac system, both neural network and conventional controllers show oscillation during the fault period. The standard controller may lose stability while the neural network controller is stable even under the unbalanced fault conditions, demonstrating an excellent adaptive capability of the neural network controller.

APPENDICES

Table 1. Network data (Fig. 7)

Component	Parameter	Value
AC system 1 & 2	Line voltage	100kV
	Frequency	60Hz
	Equivalent resistance	7.6mΩ
	Equivalent inductance	0.154mH
DC system	Voltage	+/- 100kV
	Frequency for Pi line specification	60Hz
	Pi line R, L, C	0.0139Ω/km, 159μH/km, 0.231μF/km
	Pi line length	75km

Table 2. VSC components, parameters (Fig. 8)

Component	Parameter	Value
Power converter	Switching frequency	6000Hz
Grid-filter	Resistance	0.75Ω
	Inductance	0.24H
DC Capacitor	Capacitance C_p, C_n	70 μF
DC filter (3 rd harmonic)	Capacitance C_p, C_n	12 μF
	Inductor (R, L)	0.1474Ω, 32.6mH
Smoothing reactor	Inductor (R, L)	0.0251Ω, 8mH

Table 3. VSC controllers, parameters
(k_p – proportional gain, k_i – integral gain)

Approach	Controller	Gain (k_p / k_i)
Conventional	Current loop	6.7 / 151.6
	dc voltage	0.0136 / 0.445
	AC bus voltage	Variable depending on voltage error signal
Neural network	Current loop	Neural network
	dc voltage	0.0136 / 0.445
	AC bus voltage	Same as the conventional

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