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1 **Predicting droplet deformation and breakup for moderate Weber**
2 **numbers**

3

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12

13 **Abstract**

14 The present work examines numerically the deformation and breakup of free falling
15 droplets subjected to a continuous cross flow. The model is based on the solution of
16 the Navier-Stokes equations coupled with the Volume of Fluid (VOF) methodology
17 utilized for tracking the droplet-air interface; an adaptive local grid refinement is
18 implemented in order to decrease the required computational cost. Neglecting initially
19 the effect of the vertical droplet motion, a 2D axisymmetric approximation is adopted
20 to shed light on influential numerical parameters. Following that, 3D simulations are

21 performed which include inertial, surface and gravitational forces. The model
22 performance is assessed by comparing the results against published experimental data
23 for the bag breakup and the sheet thinning breakup regimes. Furthermore, a
24 parametric study reveals the model capabilities for a wider range of Weber numbers.
25 It is proved that the model is capable of capturing qualitatively the breakup process,
26 while the numerical parameters that best predict the experimental data are identified.

27 **Keywords:** droplet breakup, VOF, adaptive grid refinement

28

29 **1 Introduction**

30 The droplet motion, deformation and breakup are interesting phenomena observed in
31 a wide variety of engineering applications including (but not limited) liquid sprays
32 injected in combustion engines. Such phenomena have attracted the interest of
33 scientists while several textbooks and review articles have addressed the relevant
34 processes (see selectively (Clift et al., 1978; Faeth et al., 1995; Gelfand, 1996;
35 Guildenbecher et al., 2009; Michaelides, 2006; Pilch and Erdman, 1987; Theofanous,
36 2011) among others)

37 The aerodynamic droplet breakup is induced as a result of an initial droplet-gas
38 relative velocity $U_{rel,0}$, and can be macroscopically characterized with the aid of well-
39 known non-dimensional numbers, namely the Weber number (We), the Reynolds
40 number (Re), the Ohnesorge number (Oh) and the density ratio (ε) (Guildenbecher et
41 al., 2009). These are defined as:

$$We = \frac{\rho_g U_{rel,0}^2 D_0}{\sigma} \quad Re = \frac{\rho_g U_{rel,0} D_0}{\mu_g} \quad Oh = \frac{\mu_l}{\sqrt{\rho_l \sigma D_0}} \quad \varepsilon = \frac{\rho_l}{\rho_g} \quad (1)$$

42 The viscosity ratio $N = \mu_l/\mu_g$ is also another influential parameter (which, however,
 43 can be derived from the above dimensionless numbers), while the Mach number can
 44 be important under certain flow conditions, which are not of interest to the present
 45 study. For low Oh numbers ($Oh < 0.1$), the droplet breakup is mainly controlled by the
 46 We number. Increase of the We number results in different regimes namely the
 47 vibrational breakup, the bag breakup, the multimode breakup, the sheet stripping (or
 48 sheet thinning) and the catastrophic breakup (Guildenbecher et al., 2009). Besides
 49 these well-defined breakup modes, the multimode breakup can be divided into
 50 intermediate breakup modes such as the bag-stamen (or bag-jet or bag/plume), the
 51 dual-bag and the plume/shear (or plume/sheet-thinning) breakup (Guildenbecher et
 52 al., 2009). For the non-dimensionalisation of time, the shear breakup timescale $\tau_{sh} =$
 53 $D_0 \sqrt{\varepsilon} / U_{rel,0}$ proposed by (Nicholls and Ranger, 1969) is widely used.

54 Several experimental studies have investigated the droplet breakup. Focusing on the
 55 aerodynamic breakup, the shock tube technique and the continuous air jet flow
 56 technique have been widely used. The shock tube technique provides a spatially
 57 uniform gas velocity by suddenly releasing pressurized gas inside a tube; the droplet
 58 deforms due to the flow field following the shock wave. This technique was used in
 59 (Hsiang and Faeth, 1992, 1993, 1995), (Chou et al., 1997), (Chou and Faeth, 1998),
 60 (Dai and Faeth, 2001) among others. The continuous air jet flow technique examines
 61 the breakup of droplets exposed to the influence of an air jet flowing from a nozzle;
 62 care is usually taken in order to minimize the boundary layer of the free jet and obtain

63 a more uniform gas velocity; see selectively (Krzeczkowski, 1980), (Liu and Reitz,
64 1997), (Lee and Reitz, 2000),(Cao et al., 2007),(Opfer et al., 2012; Opfer et al., 2014),
65 (Flock et al., 2012), (Zhao et al., 2010; Zhao et al., 2013), (Guildenbecher and Sojka,
66 2011), (Jain et al., 2015) among others. Details for these techniques can be found in
67 (Guildenbecher et al., 2009) among others. These techniques are usually applied to
68 millimeter size droplets under atmospheric conditions; as a result, high liquid/gas
69 density ratios are examined.

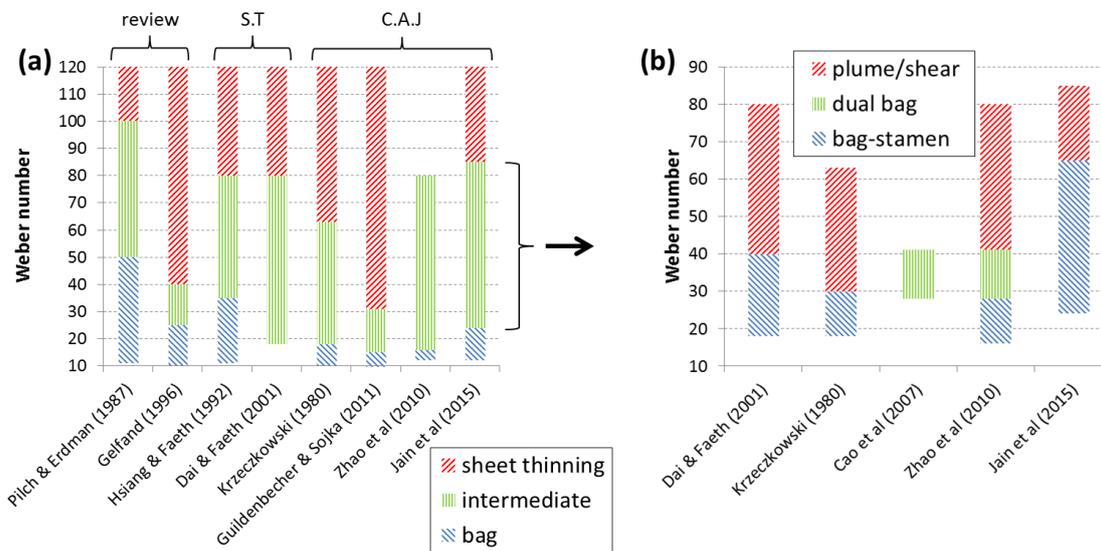
70 Krzeczowski (Krzeczkowski, 1980) used a continuous air jet to study the breakup of
71 various liquids for We numbers in the range 13.5-163 and $Oh < 3$ and he was one of the
72 first who represented the breakup regimes in the $Oh-We$ diagram. He focused on the
73 kinematics of droplet breakup and to the breakup duration and concluded that the
74 viscosity ratio plays a minor role. In a later series of studies, (Hsiang and Faeth, 1992,
75 1993, 1995) used the shock tube experimental technique to study the droplet breakup
76 at atmospheric conditions. They examined droplets of various liquids covering a wide
77 range of We , Oh and Re numbers ($We=0.5-600$, $Oh < 560$, $Re > 300$). Their results were
78 also combined with the results of previous works to finally derive the various
79 outcomes as a function of the aforementioned parameters. Drop deformation and
80 breakup regimes were presented in $Oh-We$ map and represent one of the most detailed
81 graphical representations. Later, the same group published a series of papers
82 examining the temporal properties of secondary breakup in specific breakup regimes
83 (Chou and Faeth, 1998; Chou et al., 1997; Dai and Faeth, 2001). Among them, in (Dai
84 and Faeth, 2001) the intermediate breakup regimes were investigated and they
85 identified the bag/plume breakup for $15 < We < 40$ and the plume/shear breakup for
86 $40 < We < 80$. The first one is quite similar to the bag-stamen breakup, while the second

87 represents a transition between the bag/plume and the sheet-thinning breakup in
88 which no bag is formed. (Cao et al., 2007) identified a new breakup mode appearing
89 only in continuous air flow experiments. They called it “dual-bag” and it is observed
90 between the bag/plume and the plume/shear breakup for $28 < We < 41$. The droplet
91 initially breaks up from its periphery and the remaining core droplet deforms into a
92 bag which breaks up again. (Lee and Reitz, 2000; Liu and Reitz, 1997) studied
93 experimentally the breakup of small diesel droplets ($D=69-198\mu\text{m}$) at atmospheric
94 temperature and pressures up to 9.2atm, achieving density ratios between 80 and 700;
95 nevertheless this had a small impact on breakup. They had a great contribution in
96 understanding the physical mechanism leading to the shear breakup, by comparing
97 cases with identical We numbers and Re numbers differing by a factor of almost 3.
98 They concluded that the shear breakup is not ought to shear stresses believed so far,
99 but rather to aerodynamic forces bending the flattened drop’s edge and creating a
100 sheet. Thus they proposed the sheet-thinning mechanism verified also by numerical
101 studies mentioned latter in this section (Han and Tryggvason, 2001; Khosla and
102 Smith, 2006; Wadhwa et al., 2007). Recently, (Opfer et al., 2012; Opfer et al., 2014)
103 studied experimentally and theoretically the bag breakup of droplets under a
104 continuous air jet flow. They found a similarity between bag breakup, drop-wall
105 impact and binary droplet collision. (Flock et al., 2012) studied experimentally the
106 droplet breakup in the bag and sheet thinning breakup modes using shadowgraphy to
107 record the instantaneous droplet shape, trajectory and mean velocity, while PIV was
108 used to quantify the gas flow motion around the droplet. They concluded that the
109 structure of the gas-phase wake may not significantly affect the transition between
110 liquid-phase breakup morphologies. The investigations of (Zhao et al., 2010)

111 performed almost at the same time as the aforementioned ones, examined
112 experimentally and theoretically the bag, bag-stamen and dual-bag breakup regimes.
113 They found that the transition between different bag-type regimes depends on the
114 ratio of maximum cross stream drop diameter to the Rayleigh-Taylor (RT) instability
115 wavelength. Later (Zhao et al., 2013) focused on bag-stamen breakup and found that
116 the stamen can be considered as the wave crest of the RT instability, while the growth
117 of stamen was found to have two stages: an initial exponential growth followed by a
118 spike growth. They also measured the size distribution of the fragment droplets,
119 which have been found to follow the log-normal or gamma distribution functions.

120 The aforementioned experimental studies provide information regarding the critical
121 We numbers leading to different breakup regimes, the duration of the phenomenon
122 and the time that the breakup initiates, the droplet drag coefficient and the size
123 distribution of the droplets after the breakup. It is apparent, however, that there is
124 scattering of the results which is probably ought to the experimental techniques used
125 and the experimental uncertainties. This is more evident for the We number ranges
126 corresponding to different breakup modes, which is shown in Fig.1 for low Oh
127 numbers below 0.1. In Fig.1a, the basic breakup regimes are shown in which the bag-
128 stamen, dual bag and plume/shear breakup regimes have been merged into an
129 “intermediate” breakup regime; the ranges corresponding to vibrational breakup and
130 the catastrophic breakup are not presented and the maximum We number shown is
131 limited to 120. On the top of this figure, the sources used are grouped into review
132 studies, shock tube (S.T.) and continuous air jet flow (C.A.J.) experiments. In Fig.1b,
133 the breakup modes observed in the “intermediate” breakup mode are in detail
134 presented, i.e. the bag-stamen, the dual bag and the plume/shear regimes; for the work

135 of (Jain et al., 2015) the bag-stamen mode includes also the bag/plume mode which
 136 are very similar (Cao et al., 2007). It is clear from Fig.1a that for a given *We* number,
 137 one has to consider also other parameters and cannot be certain for the breakup
 138 outcome. The scattering of the critical *We* number was also reported in the review
 139 study of (Guildenbecher et al., 2009) as also in the works of (Jalaal and Mehravaran,
 140 2012) and (Kékesi et al., 2014). It has also to be noted that the data shown in Fig.1
 141 were collected from studies aiming to define the boundaries between different
 142 breakup modes and do not include studies with a different orientation. Considering
 143 also these studies creates even more confusion, since the work of (Lee and Reitz,
 144 2000; Liu and Reitz, 1997) identified bag breakup for high *We* numbers equal to 56
 145 and 72 and (Flock et al., 2012) identified sheet thinning breakup at a low *We* number
 146 equal to 32.



147

148 Fig.1: (a) *We* numbers ranges corresponding to the basic breakup regimes ($Oh < 0.1$).
 149 The breakup modes between the bag breakup and the sheet thinning breakup have
 150 been merged into the “intermediate” breakup. In (b) the breakup modes observed into
 151 the “intermediate” breakup mode are shown. The data presented in (a) have been

152 grouped into review studies, shock tube (S.T.) and continuous air jet (C.A.J.)
153 experiments.

154 Turning now to computational and theoretical studies, a large number of works have
155 been performed, shedding light into the relevant flow processes taking place during
156 droplet breakup; here focus is given on the works referring to the breakup induced by
157 an initial droplet-gas velocity and not the breakup of free falling droplets. (Han and
158 Tryggvason, 2001) studied the breakup of impulsively accelerated droplets by using a
159 front tracking scheme in 2D axisymmetric coordinates. They assumed Diesel engines
160 conditions for low density ratios and examined various combinations of We and Re
161 numbers. They found that the critical We number separating different breakup modes
162 decreases with increasing Re number. (Aalburg, 2002) used a 2D axisymmetric Level
163 Set method to study the deformation of droplets for a wide range of We and Oh
164 numbers at small density ratios and Re numbers corresponding to steady-state laminar
165 flow conditions. It was proved that a density ratio above 32 does not affect the droplet
166 deformation and suggested a new regime map by using the coordinates $We^{1/2}/Oh -$
167 $1/Oh$ as being quite robust with the different breakup boundaries to remain almost
168 constant for $Oh \gg 1$. (Khosla and Smith, 2006) performed simulations with the VOF
169 methodology in 2D axisymmetric and 3D computational domain. After validating
170 their model qualitatively against experimental data, they concluded that droplet
171 breakup in air crossflow is ought to surface waves instead of the boundary layer
172 stripping mechanism. (Quan and Schmidt, 2006) used a moving mesh interface
173 tracking scheme with mesh adaption techniques to simulate impulsively accelerated
174 droplets. They found that the total drag coefficients are larger than typical steady-state
175 drag coefficients of solid spheres at the same Re numbers which is explained by the

176 large recirculation region behind the deformed droplet. Later (Quan, 2009) used the
177 same model to examine the interaction between two impulsively accelerated droplets
178 as a function of the distance between them. (Wadhwa et al., 2007) studied numerically
179 the transient deformation and drag of decelerating droplets in axisymmetric flows for
180 constant Re number. They found that the droplet deformation and the total drag
181 increase with increasing We number and decreasing Oh number. (Xiao, 2012; Xiao et
182 al., 2012) used a 3D-CLSVOF-LES model to study the primary breakup of liquid jets.
183 To validate their model they examined the secondary droplet breakup in the bag and
184 the sheet-thinning breakup regime (at non-turbulent conditions) showing a good
185 qualitative agreement against experimental photos. (Khare and Yang, 2013) examined
186 the drag coefficients of deforming and fragmenting droplets by using a 3D VOF-DNS
187 methodology with adaptive mesh for a broad range of We and Re numbers
188 corresponding to bag, multimode and shear breakup conditions. The drag coefficient
189 exhibits a transient behavior, since it initially increases due to droplet deformation and
190 then decreases at the initiation of breakup, while the time-averaged drag coefficient
191 decreases with increasing We number. (Jalaal and Mehravaran, 2014) studied
192 numerically and analytically the transient growth of droplet instabilities at conditions
193 corresponding to shear breakup. They employed the VOF methodology in 2D and 3D
194 cases; their model was able to capture the different modes of instabilities occurring
195 during droplet breakup. Besides the Kelvin-Helmholtz instability, the 3D simulations
196 have revealed the presence of one more type of instability, i.e the transverse azimuthal
197 modulation or the Rayleigh-Taylor instability. (Kékesi et al., 2014) used a 3D VOF
198 methodology to study the droplet deformation for low We numbers below 12 and the
199 droplet breakup for $We=20$. For the breakup case they examined the effect of density

200 ratio ($20 < \varepsilon < 80$), viscosity ratio (0.5-50) and the effect of Re number ($20 < Re < 200$).
201 For the $We=20$ case, depending on the combination of the aforementioned parameters
202 they identified the bag breakup, the shear breakup (despite the low We number) and 5
203 intermediate modes appearing for first time in literature. They proposed a new
204 breakup map in the $Re - N/\sqrt{\varepsilon}$ plane and concluded that any breakup regime can be
205 observed in the proposed map, irrespective of the We number, which however
206 contradicts previous experimental and numerical findings. (Jain et al., 2015) studied
207 experimentally and numerically with a 3D VOF methodology the breakup of small
208 water droplets ($D=230\mu\text{m}$) for We numbers in the range 20-120 capturing a wide
209 range of breakup modes. They observed an interesting transition regime between bag
210 and shear breakup for $We = 80$ and a different drop size distribution after the breakup
211 for low and high We cases; this is probably the most detailed study reported so far.
212 Recently, (Yang et al., 2016) used a variant of the CLSVOF methodology to study the
213 effect of density ratio ($\varepsilon=10-60$) on the droplet breakup for a high We number of 225.
214 They have shown that breakup is affected by the density ratio beyond the $\varepsilon=32$
215 suggested by (Aalburg, 2002) mainly by altering the topology of the gas phase
216 recirculation, while the effect of density ratio is not monotonic.

217 A common feature of the most of the aforementioned studies is that the CFD models
218 used were mainly validated qualitatively against experimental observations for the
219 droplet shape at various breakup regimes. They usually examine low density ratios in
220 order to achieve smaller breakup timescale τ_{br} ; otherwise a longer physical time has to
221 be simulated as also an even more finer mesh would be required (Jalaal and
222 Mehravaran, 2014). Among them, the 3D VOF simulations obtained with the Gerris
223 code (Jain et al., 2015; Jalaal and Mehravaran, 2014; Khare and Yang, 2013) and the

224 work of (Yang et al., 2016) with the OpenFoam code are the most impressive. The
225 grid used is dense in the order of 100-200 cells per radius (cpR); thus the underlying
226 physics behind droplet breakup could be revealed. On the other hand, the physical
227 parameters selected (e.g the density and viscosity ratio) do not allow for direct
228 comparison with experimental results and thus they were qualitatively validated; the
229 work of (Jain et al., 2015) is an exception since their model was successfully
230 validated against their own experimental results.

231 The present work examines numerically the breakup process of droplets at moderate
232 We numbers ($We=13$ and 32) subjected to a steady-state cross flow and compares the
233 model results against the detailed experimental measurements of (Flock et al., 2012)
234 for the droplet deformation. The numerical model uses the VOF methodology in both
235 2D axisymmetric and 3D computational domains; the latter accounts for the bi-axial
236 droplet motion and deformation, which is usually neglected. The following sections
237 include initially a brief description of the CFD model and the numerical setup,
238 followed by the results and their assessment which aim to shed light into the physical
239 and numerical parameters that affect the model predictions. The conclusions of the
240 present work are summarized at the end.

241

242 **2 Numerical model and methodology**

243 The numerical model solves the Navier-Stokes equations while the gas-liquid
244 interface is tracked by using the VOF methodology as described recently by the group
245 of authors in (Margarinos et al., 2015; Margarinos et al., 2014). To enhance the
246 accuracy of computations with a low computational cost, an automatic local grid

247 refinement technique is used based on the work of (Theodorakakos and Bergeles,
248 2004) and implemented as in (Malgarinos et al., 2014). To minimize the diffusion of
249 the interface, an iterative sharpening technique is implemented at the end of each
250 timestep as in (Strotos et al., 2015).

251 The simulations were performed with the commercial CFD tool ANSYS FLUENT
252 v14.5 (ANSYS®FLUENT, 2012) along with various user defined functions (UDFs)
253 for the implementation of the adaptive local grid refinement, the sharpening technique
254 and the adaptive timestep for the implicit VOF solver mentioned latter in the text. The
255 following “reference” settings have been considered as starting point: Laminar flow,
256 explicit VOF solution with the CICSAM discretization scheme (Ubbink, 1997),
257 moving grid with automatic local grid refinement, Second Order Upwind
258 discretization for the momentum equations (Barth and Jespersen, 1989), PRESTO
259 pressure interpolation scheme (ANSYS®FLUENT, 2012), velocity-pressure coupling
260 with the PISO algorithm (Issa, 1986), variable timestep with Courant number $C=0.25$
261 both for the interface tracking and the whole computational domain (global Courant
262 number).

263 In addition to the explicit VOF solver, the implicit VOF solver was also examined in
264 which the momentum and the volume tracking equations are solved simultaneously in
265 every iteration and much higher timesteps are allowed. The numerical settings
266 adopted for the implicit VOF solver was to use the Compressive discretization scheme
267 for the interface tracking, while for the temporal discretization the Bounded Second
268 Order Implicit formulation was used (ANSYS®FLUENT, 2012). A UDF was
269 implemented in order to achieve a variable timestep by assuming high Courant

270 numbers (calculated as in (Ubbink, 1997)) in the range $C=1-3$; the computational cost
 271 decreases by almost $1/C$. A list of the settings adopted for the two VOF solvers
 272 (explicit and implicit) is given in Table 1.

273

274 Table 1: List of the numerical settings adopted for the explicit and the implicit VOF
 275 solver.

	Explicit	Implicit
Temporal discretization	First Order Implicit	Bounded Second Order Implicit
Time-step	Variable ($C=0.25$)	Variable ($C=2.0$)
VOF discretization	CICSAM	Compressive
Momentum discretization	Second Order Upwind	Second Order Upwind
pressure interp. scheme	PRESTO or BFW	PRESTO or BFW
velocity-pressure coupling	PISO	PISO

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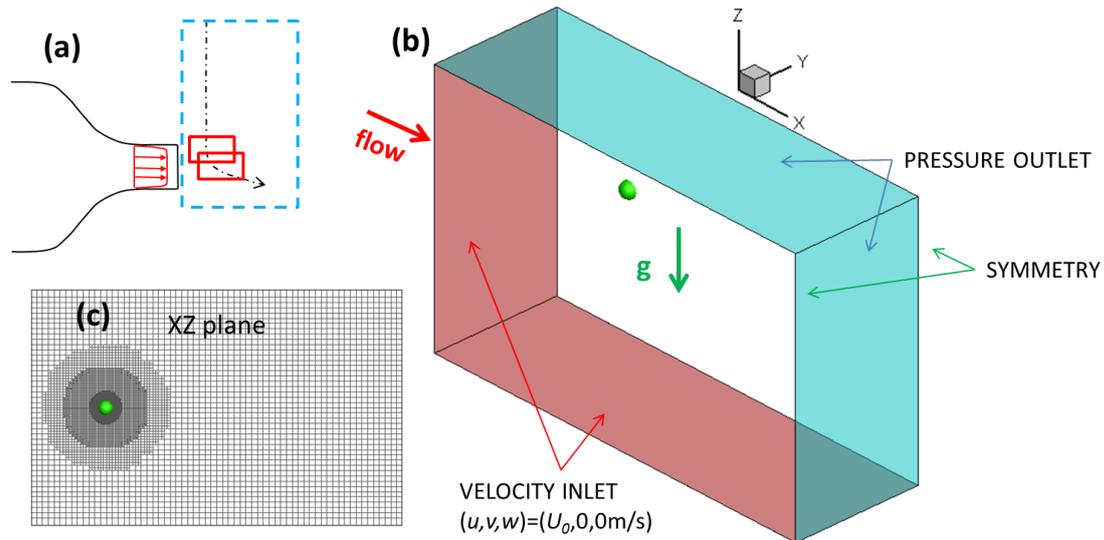
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278 **3 Results and discussion**

279 **3.1 Cases examined and numerical setup**

280 The model performance was assessed by comparing the numerical results against the
281 experimental data of (Flock et al., 2012) for the bag breakup regime ($We=13$) and the
282 sheet thinning breakup regime ($We=32$). (Flock et al., 2012) examined ethyl alcohol
283 droplets ($D=2.33\text{mm}$, $Oh=0.0059$) injected inside a continuous air jet flow with
284 adjustable velocity leading to different breakup regimes. For the case of bag breakup,
285 the mean air velocity was set equal to 10m/s resulting in $We=13$ and $Re=1500$, while
286 for the sheet thinning breakup regime the corresponding values were 16m/s , 32 and
287 2500 respectively. The droplets were falling from a height of 175mm above the air jet
288 and had a downward velocity approximately equal to 1.85m/s when they approach its
289 area of influence; the experimental configuration of (Flock et al., 2012) is shown in
290 Fig.2a in which the droplet trajectory is denoted with a dashed dotted arrow. The
291 droplet shape, trajectory and dimensions were monitored with the aid of high-speed
292 shadowgraphy (HSS), while Particle Image Velocimetry (PIV) was used to provide
293 information for the gas velocity and streamlines. The experimental measurements
294 include both mean and standard deviation values. Equally important for the
295 predictions, is the fact that the initial and boundary conditions are well defined.

296



297

298 Fig.2: (a) sketch of the experimental setup of (Flock et al., 2012), (b) computational
 299 domain and boundary conditions used for the 3D simulations, (c) computational grid
 300 at the symmetry plane.

301

302 Ideally, a large static computational domain (shown as dashed, blue rectangle in
 303 Fig.2a) with the appropriate boundary conditions at the region of the nozzle would be
 304 required to simulate the experiment. However, the large size of the computational
 305 domain would dramatically increase the computational cost, having also in mind that
 306 approximately 190ms are required for the free falling droplet to enter inside the air jet;
 307 this time interval is rather long when compared to the overall 10-12ms duration (for
 308 the $We=13$ case) of the droplet deformation and breakup process that needs to be
 309 simulated. So, the strategy adopted in the present work, was to use a small
 310 computational domain (solid, red rectangles in Fig.2a) moving with the average
 311 droplet velocity vector. The simulations start at the instance when the droplet enters
 312 the air jet assuming a step change of the gas phase velocity; the droplet is initially
 313 assumed to be spherical with a downward velocity equal to 1.85m/s. The spherical

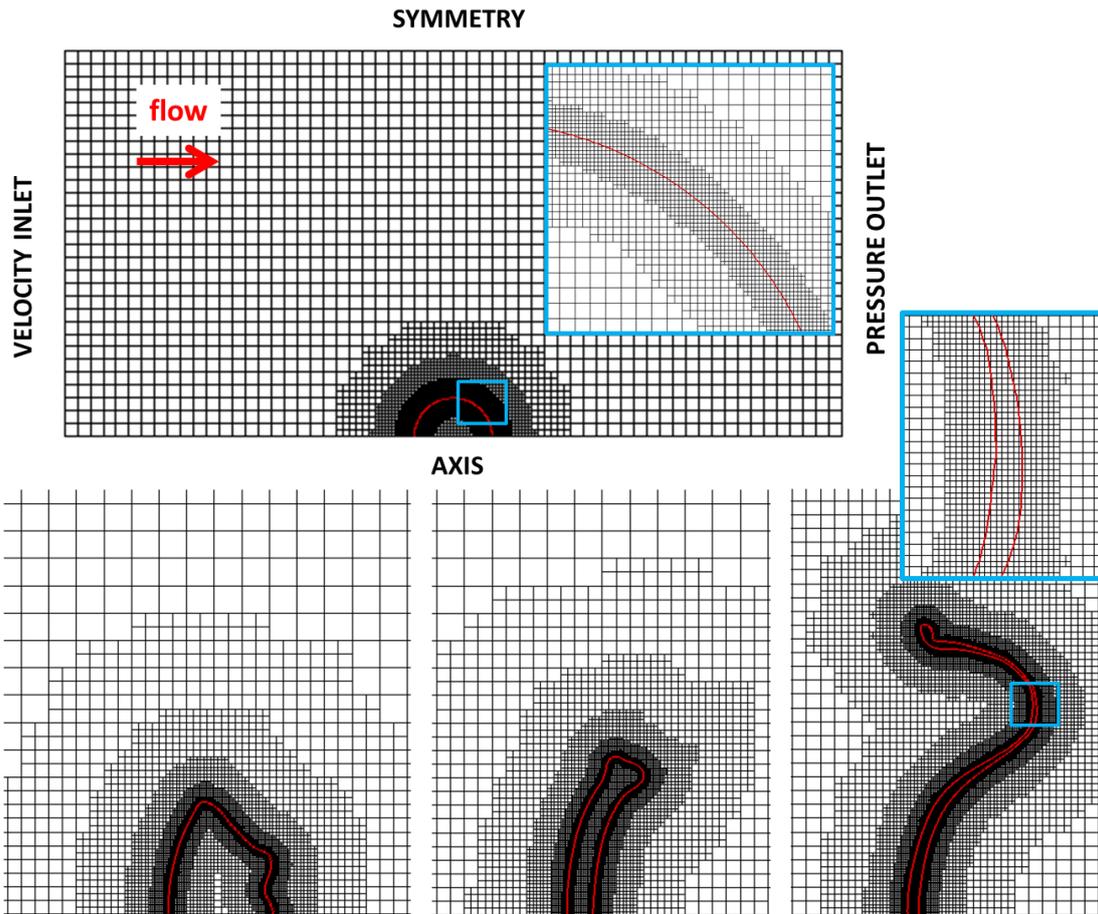
314 droplet assumption might affect the predictions as well as the initial droplet
315 perturbation when exiting the orifice might affect the overall droplet deformation;
316 however, as no information regarding these points was provided in (Flock et al.,
317 2012), the effect of these parameters was not examined.

318 The computational domain along with the boundary conditions used for the 3D
319 simulations is shown in Fig.2b. The boundaries have been placed $16R_0$ far from the
320 droplet in the YZ plane and $40R_0$ far downwind the droplet in order to minimize their
321 effect on the numerical results. In an effort to further reduce the computational cost,
322 only half of the droplet is simulated applying symmetry boundary conditions.
323 Adopting this assumption, results in ignoring possible vortex shedding in the XY
324 plane (which can be expected due to the Re number of the flow); however, this
325 assumption is supported by the relevant experimental data of (Flock et al., 2012),
326 which, judging from the PIV measurements, suggest that the structure of the wake
327 behind the droplet plays rather a minor role. The grid topology in the XZ symmetry
328 plane is shown in Fig.2c. It consists of 2 levels of static local refinement and 4 levels
329 of dynamic local refinement which finally resulted in a grid density of $96cpR$ at the
330 vicinity of the droplet interface; the static refinement was used to improve the load
331 balance between the nodes used for parallel processing. The total number of cells was
332 1.1-2.8M depending on the droplet deformation. The computational cost for the
333 explicit VOF solver was approximately 105cpu-days/ms (i.e 35days in 36 nodes to
334 simulate 12ms), while the implicit VOF solver requires significantly lower
335 computational cost (25cpu-days/ms for a global Courant number equal to 2). It has to
336 be noted that the computational cost for a denser grid of $192cpR$ increases at least by
337 a factor of 7, since the number of the computational cells increases at least by a factor

338 of 3.5 (based on a spherical droplet) with a timestep decrease by a factor of 2.
339 Nevertheless, the purpose of the 3D simulations is to identify if reasonable predictions
340 can be obtained, even with a relatively coarse grid of 96cpR.

341 Apart from the computationally expensive 3D simulations, useful information with
342 low computational cost can be obtained by using 2D axisymmetric domains which
343 ignore the vertical droplet motion and the gravitational forces, the vortex shedding
344 behind the droplet and the 3D structures during breakup. The computational grid and
345 the boundary conditions used for the 2D simulations are shown in Fig.3; for reasons
346 of distinctness, the coarse grid with 5 levels of local grid refinement (96cpR) is
347 shown, but simulations were also performed with 6 and 7 levels of local refinement
348 (corresponding to 192 and 384cpR respectively). The lower part of Fig.3 shows the
349 adaption of the grid to the droplet interface (red line corresponding to VOF=0.5),
350 while the inset figures aim to clarify the grid topology near the interface; those grids
351 correspond to the case with $We=32$.

352



353

354 Fig.3: Computational grid and boundary conditions for the 2D simulations. (5 levels
 355 of local grid refinement, 96cpR)

356

357 The 2D simulations were conducted on a computational domain moving with the
 358 instantaneous average droplet velocity; the droplet is initially motionless and it is
 359 suddenly subjected to a step change of the gas phase velocity. Upstream of the
 360 droplet, a fixed absolute velocity equal to 10m/s (or 16m/s) and downstream a fixed
 361 pressure profile equal to 1atm have been applied respectively. Note that adopting a
 362 moving computational domain with a step change of the gas phase velocity (both for
 363 the 2D and 3D simulations), results in ignoring the transitional period in which the

364 droplet enters the continuous air jet flow; nevertheless this period is quite short and it
 365 not expected to affect the model performance. A complete list of the assumptions
 366 adopted in the present work is listed in Table 2 for the 2D and the 3D simulations;
 367 these arise either from the limited computational resources (for the 3D simulations),
 368 or from the nature of the 2D simulations.

369

370 Table 2: List of the assumptions adopted for the 2D and the 3D model.

Simplification assumption	2D	3D	Expected impact
Coarse grid		√	high
Ignoring 3D structures	√		high (near breakup)
Ignoring vortex shedding	√	√ (in XZ plane)	medium
Ignoring vertical droplet motion and gravitational forces	√		medium
Initially spherical droplet	√	√	medium
Ignoring droplet motion prior entering the air jet	√	√	low
Step change of gas phase velocity	√	√	low

371

372

373 The results obtained with the 2D axisymmetric model are presented in section 3.2,
 374 while the more representative of the real conditions 3D results are presented in section
 375 3.3. In section 3.4 a parametric study for a wider range of We numbers is performed
 376 and an overall discussion of the results obtained with these approaches is performed
 377 in section 3.5. A list of the cases examined is given in Table 3.

378

379

380 Table 3: List of the cases examined.

	2D	3D
We=13 (bag)	EXPL/IMPL, PRESTO/BFW	EXPL/IMPL, PRESTO/BFW
We=32 (sheet)	EXPL/IMPL, PRESTO/BFW	EXPL/IMPL, PRESTO/BFW
We=15-90 (parametric)	EXPL, PRESTO	

381

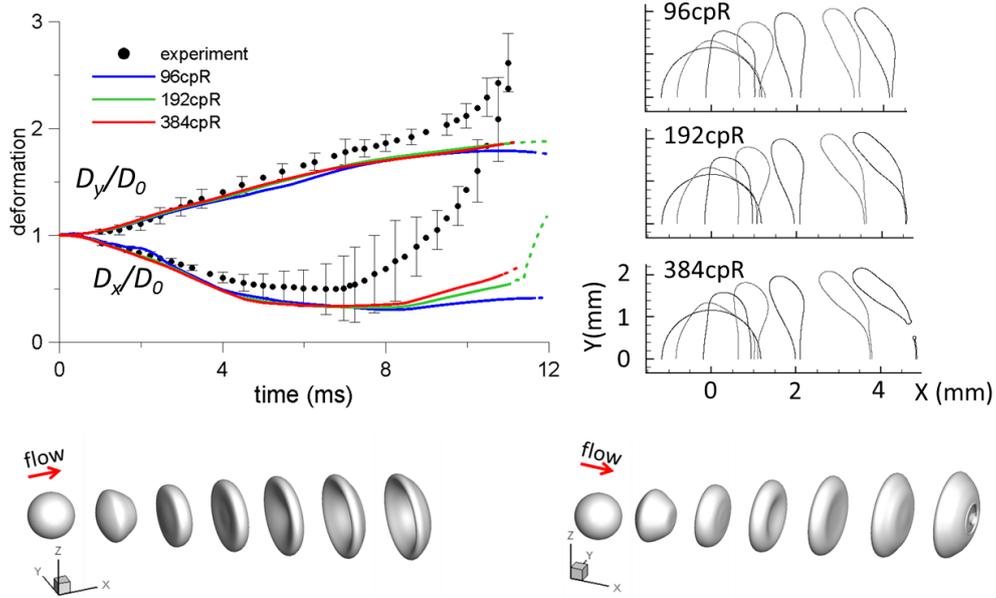
382

383 **3.2 2D simulations**

384 The results of the present 2D model for the bag breakup case ($We=13$) are presented
385 in Fig.4 for three different grid sizes namely 96, 192 and 384cpR. On the left-hand-
386 side of the figure, the predicted dimensionless droplet dimensions in the stream-wise
387 direction x and the cross-stream direction y (denoted with solid lines which turn into
388 dashed after the droplet breakup) are compared against those reported by (Flock et al.,
389 2012); error bars for the standard deviation of the measurements are also given, while
390 the experimental time has been shifted by 1ms since the experimental time $t=0$
391 corresponds to a slightly deformed droplet. On the right-hand-side of Fig.4 typical
392 droplet shapes are shown, assuming the $VOF=0.5$ to represent the droplet interface
393 and at the lower part of Fig.4 a three-dimensional representation of the breakup

394 process is shown; this was obtained by revolving the 0.5 VOF iso-value around the
395 symmetry axis. The differences for the droplet shape can be regarded as grid
396 independent during the flattening phase ($t < 7\text{ms}$), while slight deviations are observed
397 during the subsequent phase of bag creation. Increasing the grid resolution results in
398 the formation of a thinner bag and shifting of the breakup point away from the axis of
399 symmetry. Nevertheless, the solution can be regarded as grid independent for values
400 higher than 192cpR, but also the 96cpR grid could be used to provide useful
401 information on droplet breakup with a lower computational cost (this was increased
402 by a factor of 2.75 when the grid resolution was doubled). On the other hand, the
403 exact droplet dimensions reported in the experiment of (Flock et al., 2012) could not
404 be captured with the axisymmetric approach, but the droplet breakup and the general
405 trend of the evolution of the droplet shape are in accordance with the experimental
406 observations. It seems that using an even denser grid than the one with 384cpR, would
407 not improve the performance of the 2D model. This is attributed to the inevitable
408 simplifications characterizing the 2D axisymmetric model. It has also to be noted that
409 the results of the 2D axisymmetric model are not affected by the adopted numerical
410 settings (i.e. discretization schemes and pressure interpolations schemes) as it was
411 shown in (Strotos et al., 2015).

412



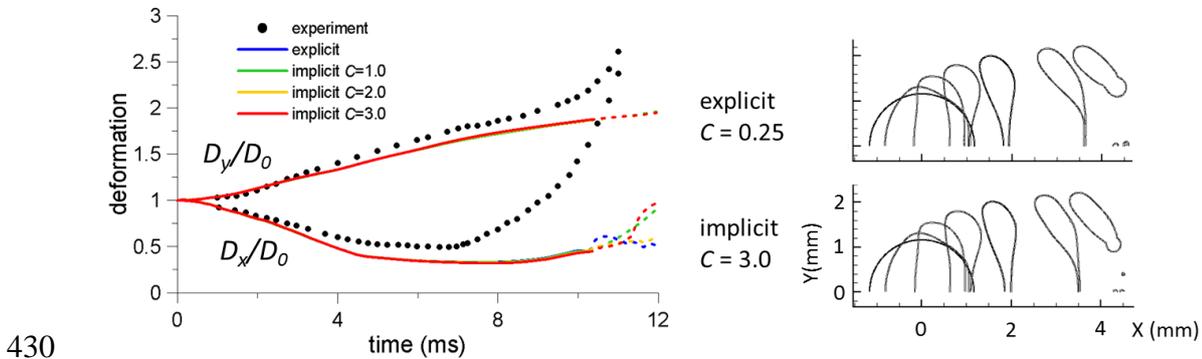
413

414 Fig.4: Temporal evolution of the droplet dimensions and droplet shapes (in intervals
 415 of 2ms) for three different grid densities ($We=13$, 2D axisymmetric domain). The last
 416 droplet shape corresponds to 11ms which is approximately the time of breakup. The
 417 bottom row shows a three-dimensional representation of the droplet shapes by
 418 revolving the 0.5 VOF iso-value.

419

420 In an effort to speed-up the calculations, the implicit VOF solver was also examined,
 421 which allows for much higher time-steps without the Courant number restriction of
 422 the explicit methodology. Variable time step was used through a user defined
 423 function; the global Courant number was kept constant, but much higher (values up to
 424 $C=3$ were examined) compared to the 0.25 value used in the explicit solver. The
 425 performance of the implicit solver for three different Courant numbers is shown in
 426 Fig.5 for the case of bag breakup with 192cpR grid. As it can be seen, it is
 427 encouraging that the global Courant number can be increased up to 3.0 with the

428 numerical accuracy remaining almost the same; some differences are observed only
 429 after the breakup.

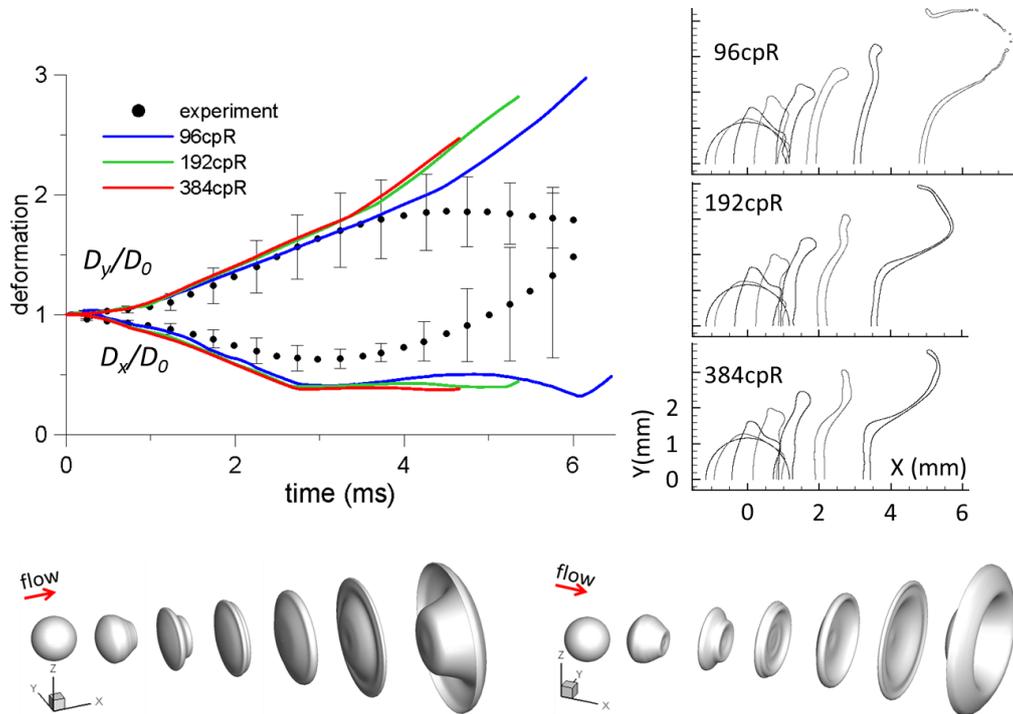


430
 431 Fig.5: Effect of implicit VOF solution in the 2D predictions of the bag breakup case
 432 ($We=13$) with the Compressive VOF discretization scheme and the sharpening
 433 algorithm.

434

435 The results of the 2D axisymmetric model for the sheet thinning breakup ($We=32$) are
 436 presented in Fig.6 for three different grid densities (96, 192 and 384cpR). As in the
 437 bag breakup case, the droplet deformation for the flattening phase ($t<3ms$) is in
 438 accordance with the experimental observations and measurements and it is not
 439 affected by the grid density. After the initial flattening phase, the solution becomes
 440 grid independent for 192cpR. But even in this case, the cross-stream deformation
 441 D_y/D_0 is over-predicted and more importantly, the droplet shape corresponds to rather
 442 a transitional regime than the sheet-thinning breakup shown in the experimental
 443 photos of (Flock et al., 2012). This transitional regime is characterized by a toroidal
 444 bag formed at the droplet periphery which eventually breaks up and it is something
 445 between the dual-bag and the plume/shear breakup regimes mentioned in the

446 introduction; these regimes are observed for $30 < We < 80$ (see Fig.1b). This point will
 447 be further analyzed in section 3.5.



448

449 Fig.6: Temporal evolution of droplet dimensions and droplet shape evolution in 1ms
 450 intervals for three different grid densities ($We=32$, 2D axisymmetric domain). The
 451 bottom row shows a three-dimensional representation of the droplet shapes by
 452 revolving the 0.5 VOF iso-value.

453

454 3.3 3D simulations

455 In this section, the results obtained with the 3D model will be presented in two
 456 separate sub-sections for the bag breakup case (section 3.3.1) and the sheet-thinning
 457 breakup case (section 3.3.2). In contrast to the 2D axisymmetric model which had a
 458 robust behavior, the 3D model performance is greatly affected by the pressure
 459 interpolation scheme. For that reason, the following sections include results from both

460 the PRESTO and the Body Force Weighted (BFW) pressure interpolation schemes, as
461 also results obtained with the implicit VOF solver which speeds-up the calculations
462 by allowing higher computational time-steps.

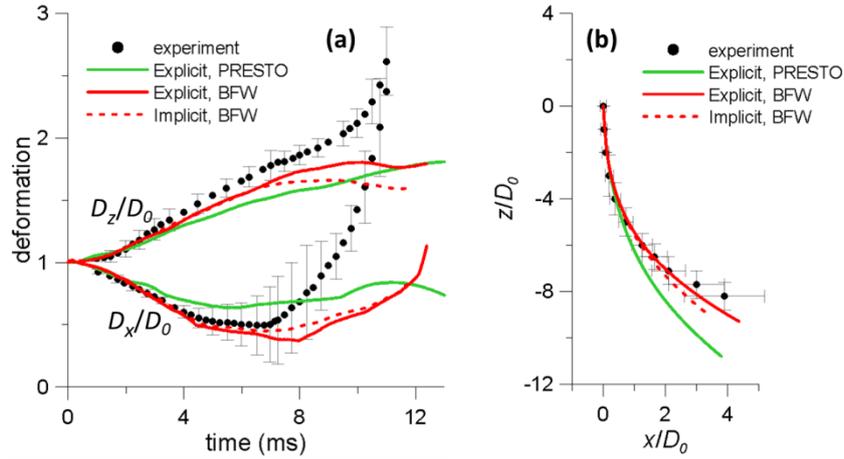
463

464 **3.3.1 Bag breakup ($We=13$)**

465 The predictions of the 3D CFD model for the droplet dimensions and the droplet
466 trajectory are shown in Fig.7 for the case of bag breakup ($We=13$). The numerical
467 settings examined are the following: (I) explicit VOF solution with either the
468 PRESTO or the BFW pressure interpolation scheme and (II) the implicit VOF
469 solution with the BFW scheme assuming a global Courant number equal to 2. The
470 flattening phase in Fig.7a is generally correctly predicted and at the bag creation
471 phase the model under-predicts the droplet deformation along the cross-stream
472 direction (z) with a lower rate of deformation in the stream-wise direction (x).
473 Examining also the predictions for the droplet trajectory (Fig.7b) it seems that the
474 explicit VOF solution with BFW pressure scheme is rather the best approach.

475

476

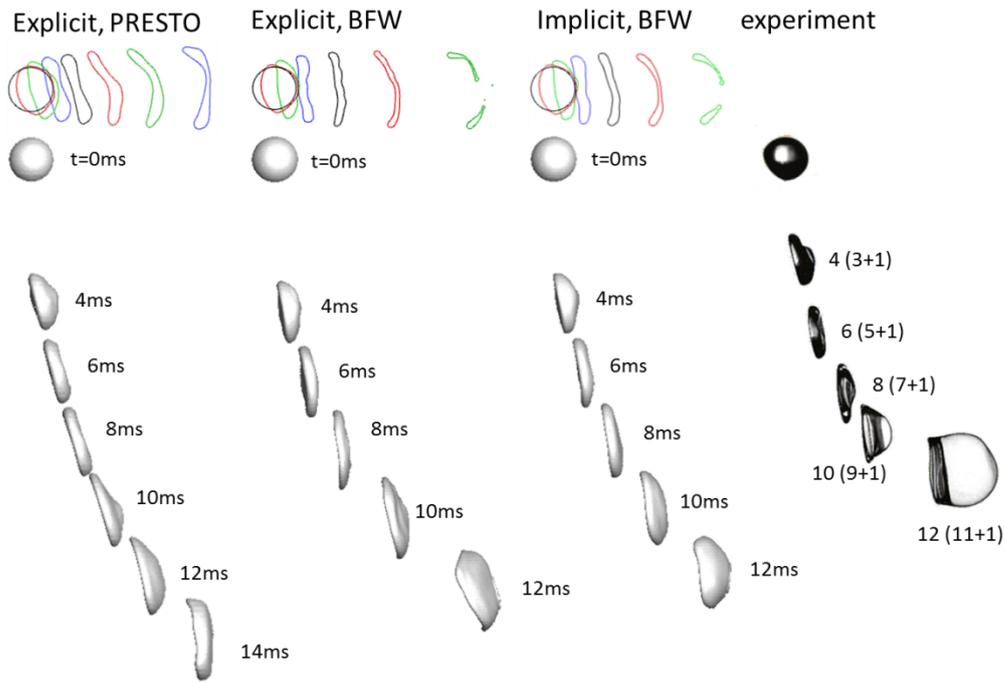


477

478 Fig.7: Predictions of the 3D model for the bag breakup case ($We=13$) for the droplet
 479 dimensions (a) and the droplet trajectory (b).

480

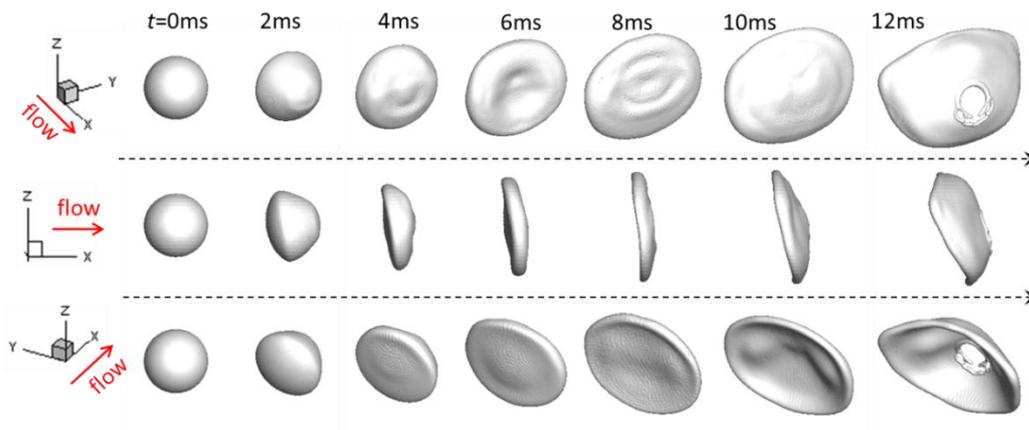
481 In contrast to the 2D simulations, the pressure interpolation scheme seems to play an
 482 important role in the 3D simulations. As a matter of fact, the PRESTO scheme
 483 exhibits higher deviation from the experimental data and it is not leading to droplet
 484 breakup. This is clearly shown in Fig.8 in which the droplet shapes in intervals of 2ms
 485 are shown. The shapes on the top row are projections of the droplet interface (xz
 486 plane) in the stream-wise direction, while the bottom row shows the actual droplet
 487 shape and position. From the top row it is evident that the PRESTO scheme does not
 488 predict breakup, while the BFW scheme (both in explicit and in implicit solution)
 489 predicts correctly the flattening ($t=0-6ms$), the bag creation ($t=8-10ms$) and the
 490 breakup ($t=12ms$). A more detailed presentation of the droplet shapes is shown in
 491 Fig.9 for the case of explicit VOF solution with the BFW scheme. The droplet
 492 deformation is presented from three different viewpoints and the characteristic phases
 493 of the bag breakup are clearly shown.



494

495 Fig.8: Predictions of the 3D model for the bag breakup case ($We=13$) for the droplet
 496 shape and trajectory (in intervals of 2ms). At the right part, the experimental photos of
 497 (Flock et al., 2012) corresponding to Figure 10 of their paper, are also shown; their
 498 experimental time has been shifted by 1ms.

499



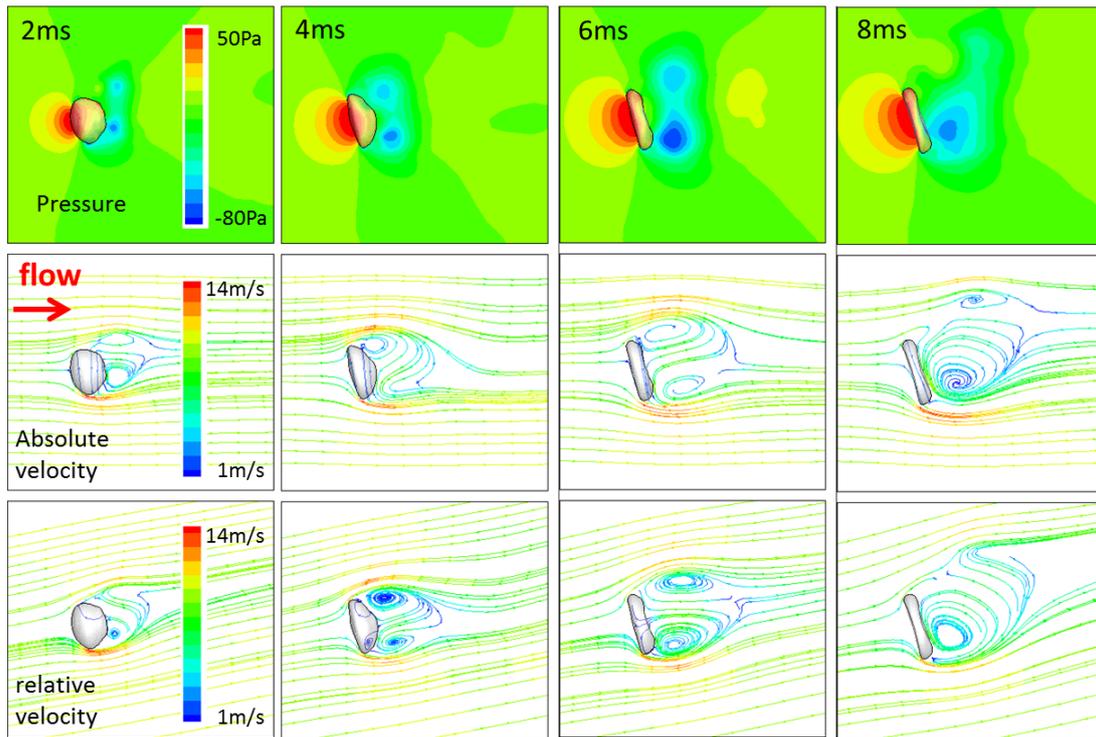
500

501 Fig.9: Different views of the droplet shape for the bag breakup case ($We=13$) in
 502 intervals of 2ms for the case of explicit VOF solution with the BFW scheme.

503

504 Focusing on the differences between the two pressure interpolation schemes, it is
505 interesting to examine the predicted flow field. This is shown in Fig.10 and Fig.11 for
506 the PRESTO and the BFW pressure interpolation schemes respectively. The 1st row of
507 the figures shows the pressure field, the 2nd row the absolute velocity streamlines and
508 the 3rd row the relative velocity streamlines; the latter are coloured with the
509 corresponding velocity magnitude and the relative velocity is obtained by subtracting
510 the velocity of the droplet from the velocity vector. Regarding the pressure field, in
511 both cases a high pressure region appears in the front stagnation point, while at the
512 rear side of the droplet low pressure regions appear at the vortex cores. Regarding the
513 velocity field (either absolute or relative), the differences between the two pressure
514 schemes are important. The PRESTO scheme predicts a quite smooth velocity field
515 with large vortical structures, which closely resembles the average velocity field
516 identified with the PIV technique in (Flock et al., 2012) (see Fig.12a). On the other
517 hand, the BFW scheme exhibits a relatively disturbed velocity field with smaller and
518 more chaotic vortices; similar eddies were identified in (Flock et al., 2012) in the
519 instantaneous (and not the averaged) velocity field (see Fig.12b). Note also that the
520 BFW scheme predicts vortex shedding, while the PRESTO scheme does not. Vortex
521 shedding is expected in this case ($Re=1500$) since it is observed for Re numbers in the
522 range $400-3 \cdot 10^5$. In (Flock et al., 2012) for the same conditions they identified
523 symmetrical vortices for some cases and alternating vortices for some other; it was
524 concluded that this point requires further experimental evidence.

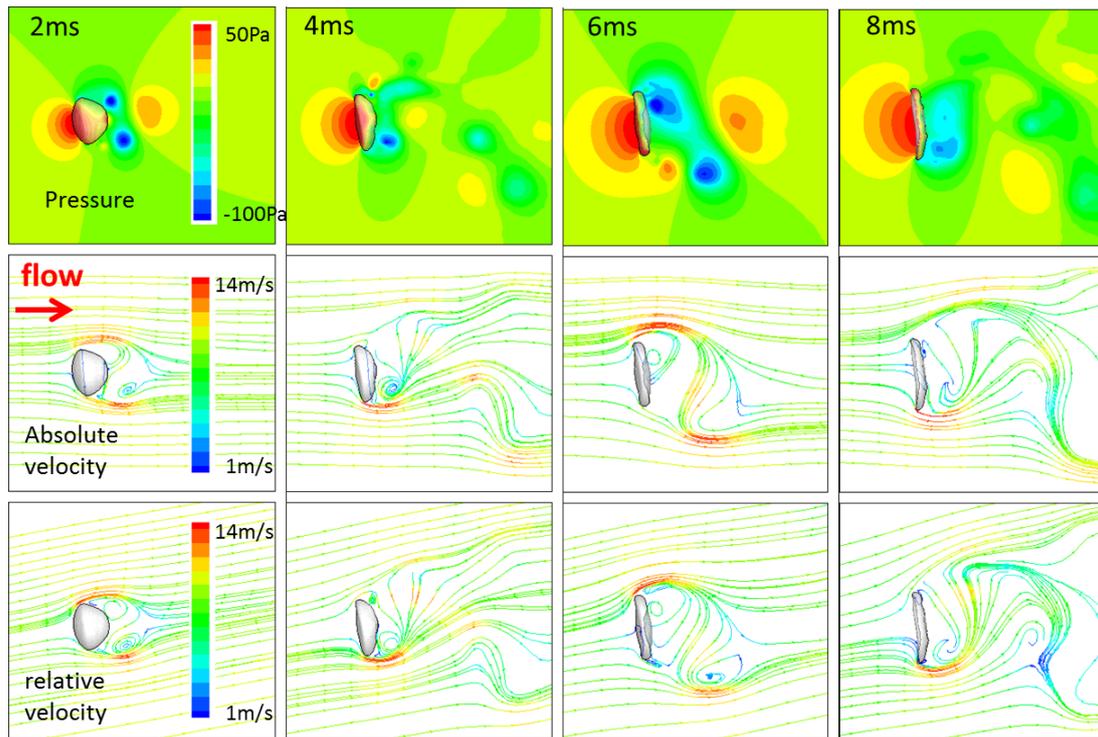
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526

527 Fig.10: Predicted pressure and velocity field for the bag breakup case ($We=13$) using
 528 the PRESTO scheme.

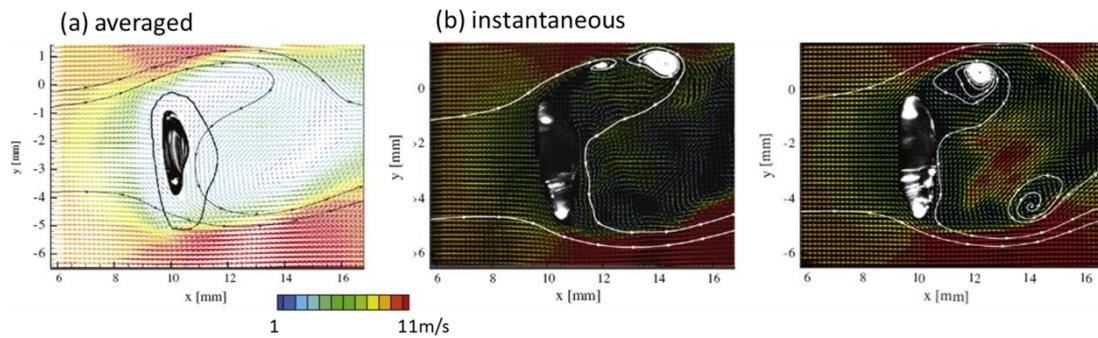
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530

531 Fig.11: Predicted pressure and velocity field for the bag breakup case ($We=13$) using
 532 the BFW scheme.

533



534

535 Fig.12: (a) Averaged and (b) instantaneous velocity field at 7ms obtained with the
 536 PIV technique in (Flock et al., 2012) for the bag breakup case ($We=13$).

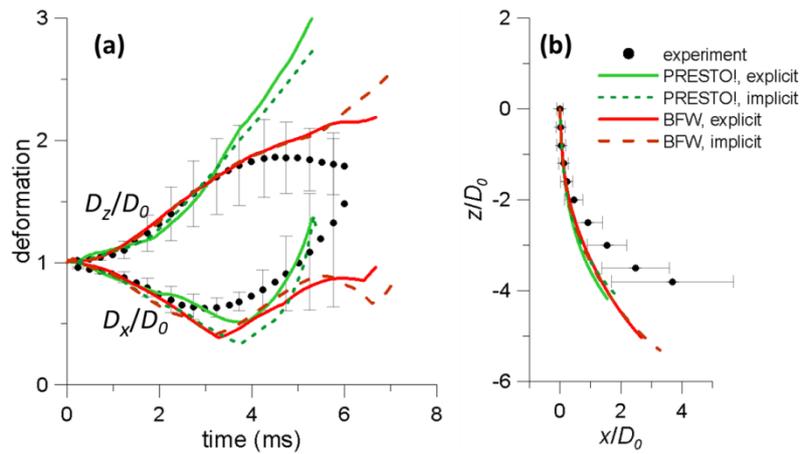
537

538 3.3.2 Sheet thinning breakup ($We=32$)

539 The predictions for the droplet dimensions and the droplet trajectory for the sheet
540 thinning breakup case ($We=32$) are shown in Fig.13. The numerical settings examined
541 are the combinations of two solution algorithms (explicit with the CICSAM
542 discretization scheme and implicit with the Compressive scheme) and two pressure
543 interpolation schemes (PRESTO and BFW). The case with the implicit solution and
544 PRESTO scheme exhibited unphysical disturbances in the interphase and was re-
545 examined with a lower global Courant number equal to 1.5. In Fig.13a the flattening
546 phase ($t<3ms$) is more or less similar for the two pressure schemes with some
547 differences after $t=2ms$ in which the BFW scheme predicts slightly higher
548 deformation. Both schemes predict the same trend with the experimental
549 measurements; nevertheless they both predict higher deformation in the stream-wise
550 direction x compared to the experimental data. In the subsequent phase of sheet
551 creation ($t>3ms$) the differences between the two pressure interpolation schemes are
552 more distinct; the PRESTO scheme exhibits higher rate of deformation compared to
553 the experimental data, while the BFW scheme predicts correctly the deformation rate
554 but the whole curve is shifted below the experimental one for the cross-stream
555 deformation due to the higher deformation predicted at the end of the flattening phase
556 ($t\sim 3ms$). At the stages near the sheet breakup ($t>4.5ms$), both schemes predict
557 increasing deformation in the z -direction (with a slightly better behaviour for the
558 BFW scheme) which contradicts the experimental data. On the other hand, similar
559 trends in increasing deformation were observed in the experimental works of (Cao et
560 al., 2007; Jain et al., 2015; Zhao et al., 2013), while the over-estimation of the cross-
561 stream diameter was also present in the detailed simulations of (Jain et al., 2015) for

562 $We=40$ and 80 . The discrepancies of the present predictions relative to the
 563 experimental data will be further discussed in section 3.5. Regarding the droplet
 564 trajectory in Fig.13b, all cases examined predict the same droplet motion which
 565 exhibits a higher velocity in the z -direction compared to the experimental one. On the
 566 other hand, the predictions for the droplet trajectory refer to the position of the mass
 567 centre, which is different from the geometric centre obtained from the outer contour
 568 of the drop shadow in (Flock et al., 2012) and does not account for the distribution of
 569 mass in the liquid structure. This fact can explain the differences between predictions
 570 and measurements in Fig.13b.

571



572

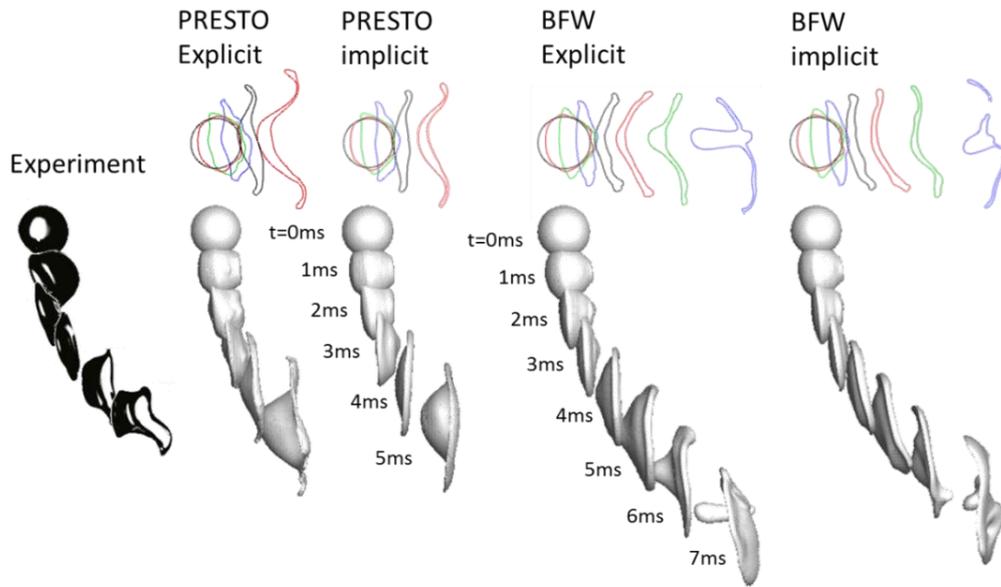
573 Fig.13: Predictions of the 3D model for the sheet thinning breakup case ($We=32$) for
 574 the droplet dimensions (a) and the droplet trajectory (b).

575

576 The side view of the predicted droplet shapes in 1ms time intervals for the four cases
 577 examined are shown in Fig.14 and detailed information on the droplet shapes from 3
 578 different viewpoints are shown in Fig.15 and Fig.16 for the PRESTO and BFW

579 schemes respectively (explicit VOF solver). All cases examined are finally leading to
580 breakup but a slightly different behaviour is observed between the PRESTO and the
581 BFW scheme after the flattening phase ($t=3\text{ms}$). The PRESTO scheme predicts the
582 formation of a sheet at the droplet periphery in the stream-wise direction while its
583 leading edge bends and forms a disc (similar droplet shapes where obtained with the
584 2D axisymmetric model); the droplet deformation is not axisymmetric (see Fig.15)
585 and this is attributed to interfacial instabilities, but also due to the symmetry boundary
586 condition which allows for vortex shedding only in the xz plane. The bend in the
587 leading edge is also present in the experimental photos of (Flock et al., 2012) but
588 seems to be more intense at the lower part of the droplet. Finally the sheet breaks up
589 at the junction of the stream-wise sheet and the leading edge. This breakup regime can
590 be regarded as the plume/shear regime. On the other hand, the BFW scheme predicts a
591 slightly different kind of deformation. The sheet formed is not changing curvature at
592 its leading edge and at $t=6\text{ms}$ the droplet deformation turns into a shape resembling
593 the bag-and-stamen regime; more details on the droplet shapes can be seen in Fig.16.
594 The accuracy of the predictions with the BFW scheme will be further discussed in
595 section 3.5.

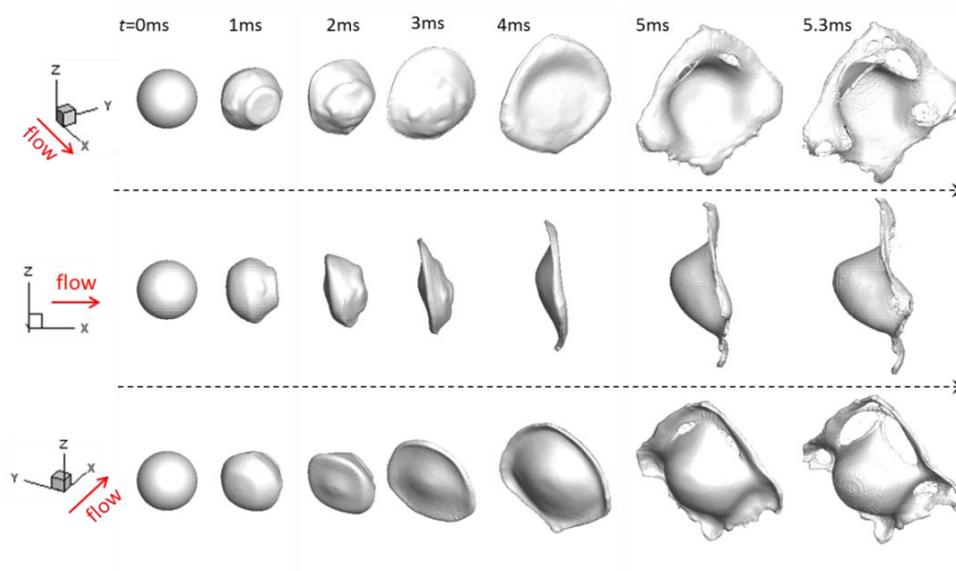
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597

598 Fig.14: Predictions of the 3D model for the sheet thinning breakup case ($We=32$) for
 599 the droplet shape and trajectory (in intervals of 1ms). At the left part, the experimental
 600 photos of (Flock et al., 2012) corresponding to Figure 15 of their paper, are also
 601 shown.

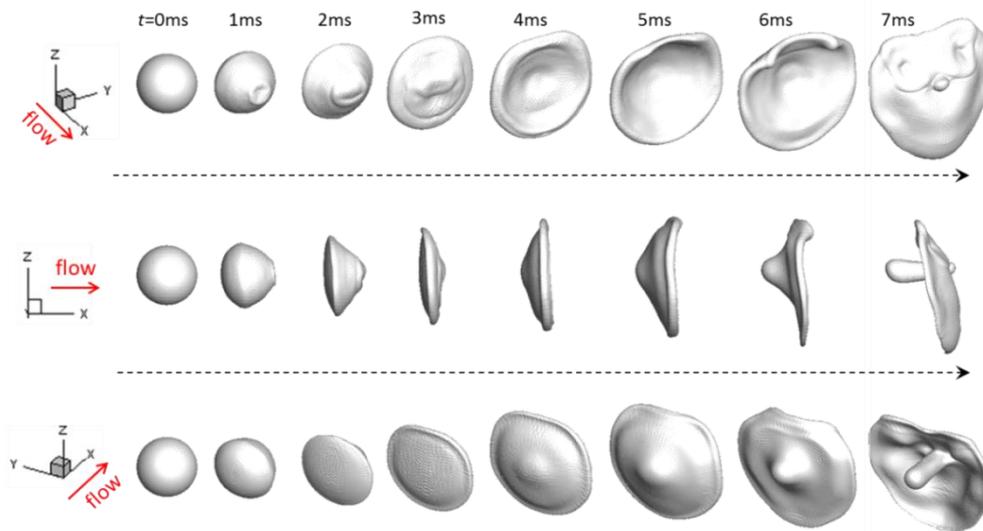
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603

604 Fig.15: Different views of the droplet shape in intervals of 1ms for the case of explicit
 605 VOF solution with the PRESTO scheme for the sheet thinning breakup case ($We=32$).

606



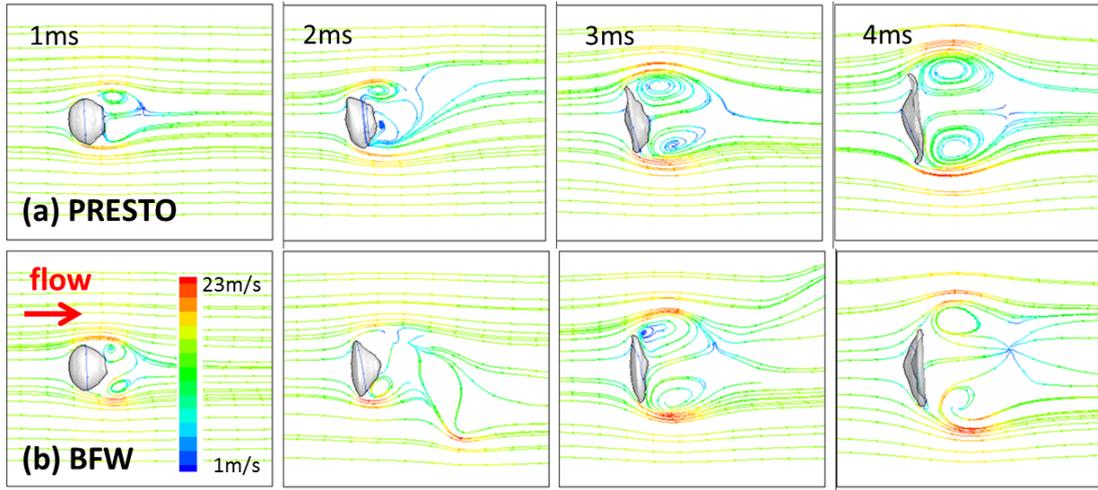
607

608 Fig.16: Different views of the droplet shape in intervals of 1ms for the case of explicit
609 VOF solution with the BFW scheme for the sheet thinning breakup case ($We=32$).

610

611 Regarding the predicted velocity field for the two pressure interpolation schemes, the
612 comments made for the bag breakup case in section 3.3.1, apply also for the sheet
613 thinning breakup case. The PRESTO scheme (Fig.17a) exhibits a rather steady-state
614 velocity field similar to the averaged one presented in (Flock et al., 2012) (see
615 Fig.18a), while the BFW scheme (Fig.17b) predicts a transient velocity field with
616 vortex shedding which is closer to the instantaneous velocity field presented in (Flock
617 et al., 2012) (see Fig.18b); this was rather expected due to the Re number of the flow
618 ($Re=2500$), but as stated in (Flock et al., 2012) this point requires more experimental
619 evidence.

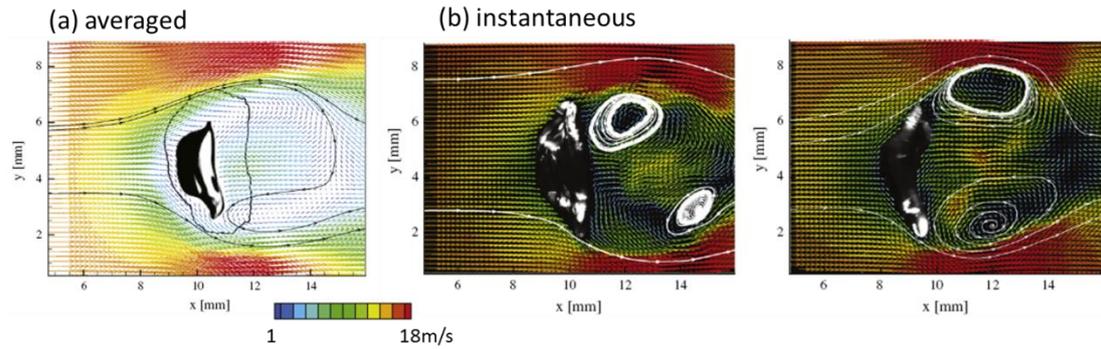
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621

622 Fig.17: Predicted absolute velocity field for the sheet thinning breakup case ($We=32$)
 623 using explicit VOF for (a) the PRESTO and (b) the BFW scheme.

624



625

626 Fig.18: Averaged (a) and instantaneous (b) velocity field at 4ms obtained with the
 627 PIV technique in (Flock et al., 2012) for the sheet thinning breakup case ($We=32$).

628

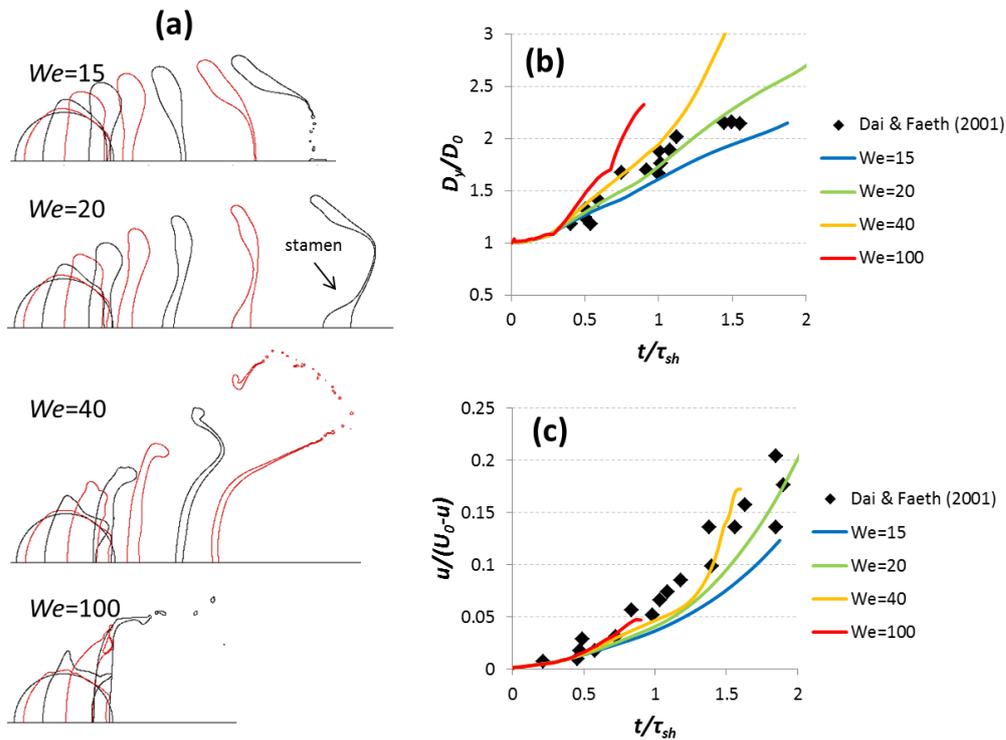
629 3.4 Parametric study

630 In an effort to further explore the model capabilities in predicting the various breakup
 631 regimes, a parametric study has been performed by examining well established We
 632 numbers which lead to the different breakup regimes presented in Fig.1. This time the

633 model performance will be assessed based on qualitative criteria without a direct
634 comparison with specific experimental data; this is a common practice to validate
635 CFD models and it was used by the majority of the studies mentioned in the
636 introduction. The conditions examined are those of (Flock et al., 2012), i.e. 2.33mm
637 ethyl alcohol droplets in air, but with a varying gas phase velocity leading to We
638 numbers 15, 20, 40 and 100 which correspond to bag, bag-stamen, transition
639 (plume/shear) and sheet-thinning breakup respectively. The simulations were
640 performed with the explicit VOF solver, CICSAM and PRESTO schemes, 192cpR
641 grid in a 2D axisymmetric domain which ignores the vortex shedding behind the
642 droplet, but as it will be seen, this is not affecting the breakup outcome. The results
643 obtained for the droplet shapes are presented in Fig.19a for time intervals of $0.05\tau_{sh}$. It
644 is clear that the model can adequately capture the various breakup regimes. For the
645 bag-stamen case ($We=20$), a relatively short stamen is predicted (similar to (Xiao,
646 2012)), while for the sheet-thinning breakup ($We=100$) one can see the interfacial
647 instabilities at the initial stages and the continuous stripping from the droplet
648 periphery during breakup; similar instabilities (Kelvin-Helmholtz and Rayleigh-
649 Taylor instabilities) were also identified in the numerical work of (Jalaal and
650 Mehravaran, 2014). In Fig.19b,c the predicted (up to the breakup instant) droplet
651 deformation and droplet velocity are presented along with the experimental data of
652 (Dai and Faeth, 2001) for $20 < We < 81$; these have been digitized and further processed
653 in order to be presented in the axes shown in Fig.19b,c. As seen, the model results
654 agree with the experimental measurements. Increasing the We number results in
655 increasing the rate of deformation as also earlier breakup which is in accordance with
656 the experimental findings of (Pilch and Erdman, 1987) and (Dai and Faeth, 2001).

657 The droplet velocity (normalized with the instantaneous drop-gas relative velocity
 658 $U_0 - u$), increases with time without a noticeable effect of We number and it is in
 659 accordance with the experimental data.

660



661

662 Fig.19: Parametric study for the effect of We number (2D axisymmetric simulations).
 663 (a) Droplet shapes corresponding to time intervals of $0.05\tau_{sh}$, (b) cross-stream droplet
 664 deformation, (c) droplet velocity.

665

666 3.5 Discussion

667 The 3D simulations presented in section 3.3 have shown that the pressure
 668 interpolation scheme (PRESTO or BFW) plays an important role, in contrast to the
 669 2D simulations which are generally insensitive on the numerical settings. The BFW

670 treats the gravitational and surface tension forces similar to the pressure forces; the
671 key assumption is the constant normal gradient to the face of the body force and
672 pressure. According to the authors, this scheme probably acts as a modified Rhie-
673 Chow algorithm (see for example (Gu, 1991) among many other pressure-correction
674 algorithms). This is expected to result to a better balance of the pressure and body
675 forces at the cell face, and thus, to a more accurate solution. The PRESTO scheme is
676 based on the classical staggered grid scheme approach as highlighted by (Patankar,
677 1980). It uses the explicit discrete continuity balance on a staggered control volume
678 around the face to compute the pressure. From the results obtained for the specific
679 cases simulated here, the main difference between the two schemes is found on the
680 predicted recirculation zones of the 3D cases, which, according to (Yang et al., 2016),
681 these can play a role during droplet breakup. The PRESTO scheme predicts a steady
682 state velocity field without vortex shedding, while the BFW scheme predicts an
683 unsteady velocity field with vortex shedding; this was expected since the Re number
684 of the cases examined is above 1500. Having also in mind that the PRESTO scheme
685 cannot predict the bag breakup, it has been concluded the BFW scheme better predicts
686 droplet breakup.

687 For the bag breakup case, both the 2D axisymmetric (up to the break-up time) and the
688 3D simulations are in accordance with the experimental observations, predicting quite
689 accurately the flattening phase and having some discrepancies in the bag creation
690 phase for which the bag dimensions are under-predicted. The 2D model which ignores
691 the forces in the vertical direction (including the gravitational one) is not able to
692 capture the secondary droplet deformation and its deviation from the axisymmetric
693 shape (see the experimental photos in Fig.8 and Fig.14). As these forces acting on the

694 vertical direction, they serve as an inception point and they further promote the
695 creation of the bag; ignoring them results in higher deviation from the experimental
696 dimensions at the latter stages of deformation (see section 3.2) compared to the 3D
697 predictions. On the other hand, the We number based on the downward droplet
698 velocity at the instance that the droplet enters the jet is 0.44 and it is two orders of
699 magnitude lower compared to the one based on the jet velocity. For that reason, the
700 influence of the downward motion is not expected to alter the general breakup
701 outcome until the break-up time; that justifies the applicability of the 2D
702 axisymmetric model for the prediction of the initial droplet deformation and break-up
703 time. Moreover, the Froude number based on its classical definition ($Fr=U^2/gD$) is
704 4374 and 11200 for the two cases examined; a modified Froude number, expressing
705 the ratio of air inertia forces over gravitational forces and defined as $\rho_g U^2 / \rho_{liq} g D$, is
706 6.82 and 17.46 for the two cases, respectively; as the resulting values are much higher
707 than unity, it can be expected that the gravitational forces play a minor role on the
708 breakup process.

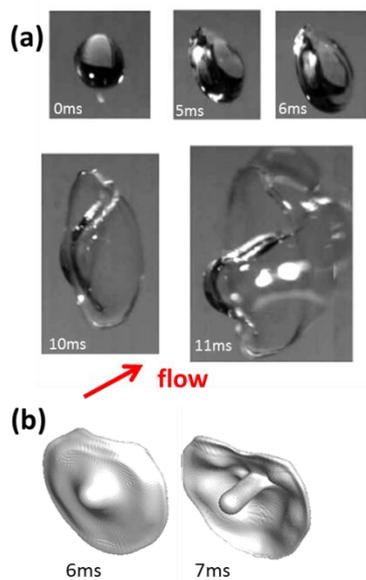
709 Regarding the 3D simulations of the bag breakup case, the discrepancies from the
710 experimental data are attributed to the simplifications made to reduce the
711 computational cost, i.e the adoption of a moving computational domain, the
712 simulation of the half of the droplet, the assumption of initially spherical droplet and
713 the usage of a relatively coarse grid (96cpR); nevertheless, we cannot a-priori
714 estimate the influence of those parameters without performing the corresponding
715 simulations. Another parameter that might affect the model performance is
716 turbulence. The Re number based on the nozzle diameter is 17100 and (Flock et al.,
717 2012) report a turbulent intensity of 1.5%. These conditions correspond rather to a

718 transitional flow than a fully turbulent and a 3D LES model (Large Eddy Simulation)
719 should be able to capture the flow structures, but the computational cost would further
720 increase, since a dense isotropic grid would be required in the whole computational
721 domain (not only near the interface) as also a lower Courant number (~ 0.2). In
722 (Strotos et al., 2015) it was shown that the RANS turbulence modelling failed to
723 predict the bag breakup, which is accordance with the findings of (Tavangar et al.,
724 2014); on the contrary, LES model was able to capture the phenomenon. Since
725 (Tavangar et al., 2014) used the same grid for both models, this reflects the
726 superiority of LES.

727 Turning now our interest to the sheet thinning breakup case, there is a qualitative
728 agreement between the 2D axisymmetric simulations and the 3D simulations with the
729 PRESTO interpolation scheme, probably due to the steady-state velocity field
730 predicted with these settings. Nevertheless, instead of the sheet thinning breakup
731 shown in the experimental photos, they both predict a plume/shear breakup. A similar
732 contradiction exists also for the 3D predictions with BFW scheme which predicts
733 something between a bag-and-stamen and a dual-bag breakup. On the other hand,
734 similar droplet shapes with the present predictions (see Fig.20a and b) were observed
735 in (Cao et al., 2007; Zhao et al., 2013) for large water droplets at $We=29$ representing
736 the so-called dual-bag breakup. As stated in the introduction, a variety of critical We
737 numbers leading to sheet-thinning breakup has been reported in literature. From figure
738 Fig.1 it seems that the We number of 32 examined corresponds rather to a transitional
739 regime than a sheet-thinning breakup which is generally observed at higher We
740 numbers above 80; nevertheless the critical We number might be affected by several

741 other parameters. It seems that the $We=32$ case is in the limit between different
 742 breakup modes and such conditions are generally difficult to be captured by CFD
 743 codes. This fact in addition to the assumptions made to reduce the computational cost
 744 may explain the different breakup regime predicted. Summarizing, the discrepancies
 745 observed relative to the experimental measurements are attributed to the assumptions
 746 made to minimize the computational cost, while the deviation in the predicted droplet
 747 shape for the higher We number case is ought to the complicated nature of droplet
 748 breakup in the range $We=20-80$, which has been reported in several past works.

749



750

751 Fig.20: (a) experimental photos of (Zhao et al., 2013) for the dual-bag breakup of
 752 water droplets for $We=29$, (b) present 3D predictions for $We=32$ with the BFW
 753 pressure scheme.

754

755 **4 Conclusions**

756 In the present work, the bag breakup and the sheet thinning breakup of droplets
757 subjected to a continuous air flow were studied with the VOF methodology in 2D
758 axisymmetric and 3D computational domains. The model results were compared
759 against experimental data showing a qualitative agreement while the discrepancies
760 observed were attributed to the simplifications made to reduce the computational cost.
761 In addition to that, a parametric study for a wider range of We numbers has shown
762 that the model can adequately predict a broad range of breakup regimes.

763 Whilst the 2D axisymmetric model had a robust behavior and it was not affected by
764 the numerical settings used for the two breakup modes examined, the 3D model was
765 greatly affected by the pressure interpolation scheme which may result in quite
766 different flow types, namely steady-state flow for the PRESTO scheme and transient
767 flow with vortex shedding for the Body Force Weighted (BFW) scheme. Furthermore,
768 the PRESTO scheme was not able to capture the 3D bag breakup case, while in the
769 higher We number case both schemes predicted breakup. To the authors' opinion, the
770 BFW scheme (either in the explicit or the implicit VOF solution) is the best choice for
771 3D calculations. It predicts breakup for both cases examined, despite the fact that for
772 the case with the higher We number a bag-stamen breakup was predicted instead of
773 the experimentally observed sheet thinning breakup; in fact this We number is rather
774 in the transitional range between different breakup modes and it is not purely
775 representing a sheet thinning breakup. Finally, the implicit VOF solution with
776 variable timestep can provide accurate results with a lower computational cost;

777 nevertheless unphysical interfacial instabilities were observed for the high We case
 778 with the 3D PRESTO scheme which were vanished by reducing the Courant number.

779

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784

785 **6 Nomenclature**

786

Roman symbols

Symbol	Description	Units
C	Courant number $C = u \cdot \delta t / \delta x$	-
D	diameter	m
g	gravitational acceleration	m/s ²
Oh	Ohnesorge number $Oh = \mu_l / \sqrt{\rho_l \sigma D_0}$	-
p	pressure	Pa
R	radius	m
Re	Reynolds number $Re = \rho_g U_{rel,0} D_0 / \mu_g$	-
t	time	s
U	reference velocity	m/s
u, v, w	velocity components	m/s
We	Weber number $We = \rho_g U_{rel,0}^2 D_0 / \sigma$	-

787

788

Greek symbols

Symbol	Description	Units
δt	timestep	s
δx	cell size	m
ε	density ratio $\varepsilon = \rho_l / \rho_g$	-
μ	viscosity	kg/ms
N	Viscosity ratio $N = \mu_l / \mu_g$	-
ρ	density	kg/m ³

σ	surface tension coefficient	N/m
τ_{sh}	Shear breakup timescale $\tau_{sh} = D\sqrt{\varepsilon}/U$	-

789

Subscripts

Symbol	Description
0	initial
g	gas
l	liquid
rel	relative
x,y,z	coordinates

790

Abbreviations

Symbol	Description
BFW	Body Force Weighted
CFD	Computational Fluid Dynamics
CICSAM	Compressive Interface Capturing scheme for Arbitrary Meshes
CLSVOF	Coupled Level-Set VOF
cpR	Cells per Radius
DNS	Direct numerical simulation
PISO	Pressure-Implicit with Splitting of Operators
PIV	Particle Image Velocimetry
PRESTO	PREssure STaggering Option
UDF	User Defined Function
VOF	Volume of Fluid

791

792 **7 References**

793

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906

907

908 **8 Figure Captions**

909 Fig.1: (a) We numbers ranges corresponding to the basic breakup regimes ($Oh < 0.1$).
910 The breakup modes between the bag breakup and the sheet thinning breakup have
911 been merged into the “intermediate” breakup. In (b) the breakup modes observed into
912 the “intermediate” breakup mode are shown. The data presented in (a) have been
913 grouped into review studies, shock tube (S.T.) and continuous air jet (C.A.J.)
914 experiments.

915

916 Fig.2: (a) sketch of the experimental setup of (Flock et al., 2012), (b) computational
917 domain and boundary conditions used for the 3D simulations, (c) computational grid
918 at the symmetry plane.

919

920 Fig.3: Computational grid and boundary conditions for the 2D simulations. (5 levels
921 of local grid refinement, 96cpR)

922

923 Fig.4: Temporal evolution of the droplet dimensions and droplet shapes (in intervals
924 of 2ms) for three different grid densities ($We=13$, 2D axisymmetric domain). The last
925 droplet shape corresponds to 11ms which is approximately the time of breakup. The
926 bottom row shows a three-dimensional representation of the droplet shapes by
927 revolving the 0.5 VOF iso-value.

928

929 Fig.5: Effect of implicit VOF solution in the 2D predictions of the bag breakup case
930 ($We=13$) with the Compressive VOF discretization scheme and the sharpening
931 algorithm.

932

933 Fig.6: Temporal evolution of droplet dimensions and droplet shape evolution in 1ms
934 intervals for three different grid densities ($We=32$, 2D axisymmetric domain). The
935 bottom row shows a three-dimensional representation of the droplet shapes by
936 revolving the 0.5 VOF iso-value.

937

938 Fig.7: Predictions of the 3D model for the bag breakup case ($We=13$) for the droplet
939 dimensions (a) and the droplet trajectory (b).

940

941 Fig.8: Predictions of the 3D model for the bag breakup case ($We=13$) for the droplet
942 shape and trajectory (in intervals of 2ms). At the right part, the experimental photos of
943 (Flock et al., 2012) corresponding to Figure 10 of their paper, are also shown; their
944 experimental time has been shifted by 1ms.

945

946 Fig.9: Different views of the droplet shape for the bag breakup case ($We=13$) in
947 intervals of 2ms for the case of explicit VOF solution with the BFW scheme.

948

949 Fig.10: Predicted pressure and velocity field for the bag breakup case ($We=13$) using
950 the PRESTO scheme.

951

952 Fig.11: Predicted pressure and velocity field for the bag breakup case ($We=13$) using
953 the BFW scheme.

954

955 Fig.12: (a) Averaged and (b) instantaneous velocity field at 7ms obtained with the
956 PIV technique in (Flock et al., 2012) for the bag breakup case ($We=13$).

957

958 Fig.13: Predictions of the 3D model for the sheet thinning breakup case ($We=32$) for
959 the droplet dimensions (a) and the droplet trajectory (b).

960

961 Fig.14: Predictions of the 3D model for the sheet thinning breakup case ($We=32$) for
962 the droplet shape and trajectory (in intervals of 1ms).

963

964 Fig.15: Different views of the droplet shape in intervals of 1ms for the case of explicit
965 VOF solution with the PRESTO scheme for the sheet thinning breakup case ($We=32$).

966

967 Fig.16: Different views of the droplet shape in intervals of 1ms for the case of explicit
968 VOF solution with the BFW scheme for the sheet thinning breakup case ($We=32$).

969

970 Fig.17: Predicted absolute velocity field for the sheet thinning breakup case ($We=32$)
971 using explicit VOF for (a) the PRESTO and (b) the BFW scheme.

972

973 Fig.18: Averaged (a) and instantaneous (b) velocity field at 4ms obtained with the
974 PIV technique in (Flock et al., 2012) for the sheet thinning breakup case ($We=32$).

975

976 Fig.19: Parametric study for the effect of We number (2D axisymmetric simulations).
977 (a) Droplet shapes corresponding to time intervals of $0.05\tau_{sh}$, (b) cross-stream droplet
978 deformation, (c) droplet velocity.

979

980 Fig.20: (a) experimental photos of (Zhao et al., 2013) for the dual-bag breakup of
981 water droplets for $We=29$, (b) present 3D predictions for $We=32$ with the BFW
982 pressure scheme.

983

984 **9 Tables**

985 Table 1: List of the numerical settings adopted for the explicit and the implicit VOF
986 solver.

987

988 Table 2: List of the assumptions adopted for the 2D and the 3D model.

989

990 Table 3: List of the cases examined.